

"Binary Number System"

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Common Powers

Prefix	Symbol	Power of 10	Power of 2	Prefix	Symbol	Power of 10
Kilo	K	1 thousand = 10^3	$2^{10} = 1024$	Milli	m	1 thousandth = 10^{-3}
Mega	М	1 million = 10^6	2 ²⁰	Micro	μ	1 millionth = 10^{-6}
Giga	G	1 billion = 10^9	2 ³⁰	Nano	n	1 billionth = 10^{-9}
Tera	Т	1 trillion = 10 ¹²	2 ⁴⁰	Pico	р	1 trillionth = 10^{-12}
Peta	Р	1 quadrillion = 10 ¹⁵	2 ⁵⁰	Femto	f	1 quadrillionth = 10^{-15}
Exa	E	1 quintillion = 10 ¹⁸	2 ⁶⁰	Atto	а	1 quintillionth = 10^{-18}
Zetta	Z	1 sextillion = 10 ²¹	2 ⁷⁰	Zepto	z	1 sextillionth = 10 ⁻²¹
Yotta	Υ	1 septillion = 10 ²⁴	2 ⁸⁰	Yocto	у	1 septillionth = 10^{-24}

2ⁿ: Byte, Memory capacity

10ⁿ: Bit, Data processing speed or data transfer speed

Bit/second: Microprocessor operating speed, speed of data transfer

Laws of Exponents

 Let a and b be positive numbers and let x and y be real numbers. Then,

$$b^x \cdot b^y = b^{x+y}$$

$$2. \qquad \frac{b^x}{b^y} = b^{x-y}$$

$$(b^x)^y = b^{xy}$$

$$(ab)^x = a^x b^x$$

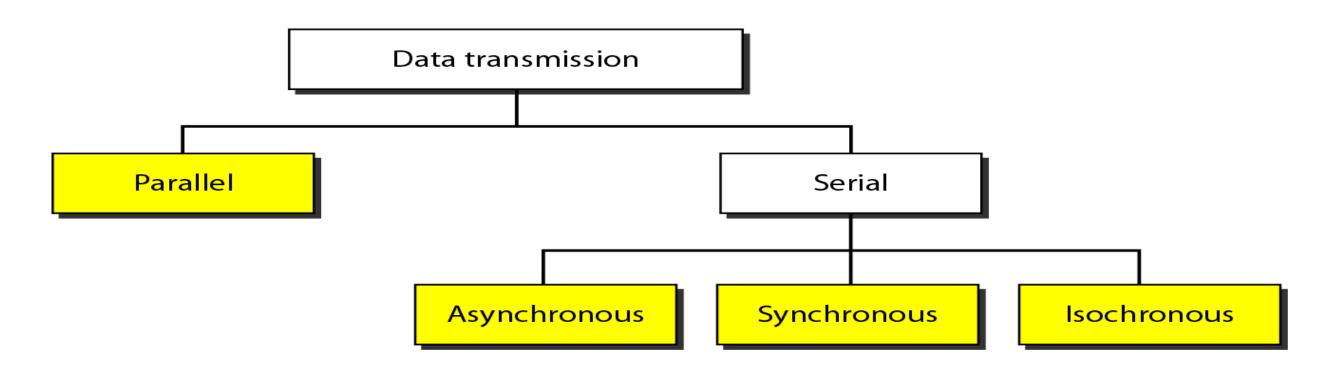
$$5. \qquad \left(\frac{a}{b}\right)^x = \frac{a^x}{b^x}$$

Computer Arithmetic Operations

- Four operations: + (-, *, /)
- Logical: AND, OR, NOT, ...
- Comparison: <, >, ≥, ≤, ==, ≠, ...
- Microprocessor ALU (Arithmetic Logic Unit) has only addition operation and performs multiplication and division operations with shift.
- Rotate / Shift left (Multiplication)
- Rotate / Shift right (Division)
- Exponential operations

Data Transmission on Computer Systems

Data transmission and modes



Serial Transmission

Data is transmitted, on a single channel, one bit at a time one after another

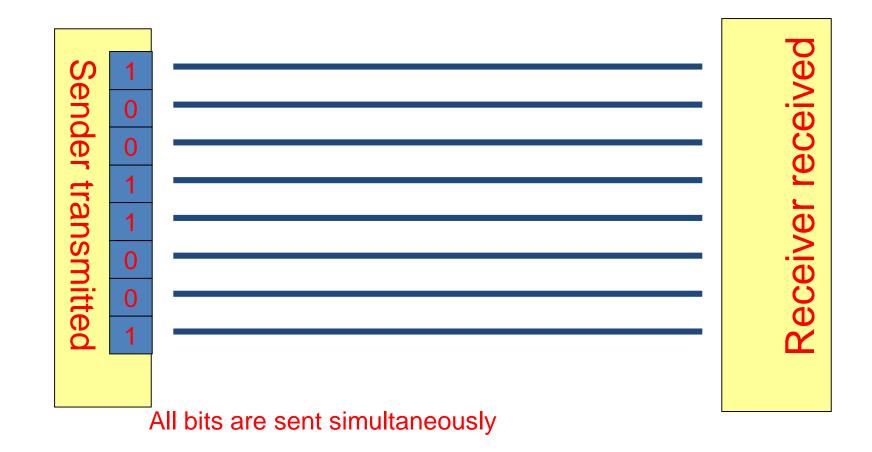
- Much faster than parallel

Sender transmitted

Receiver received

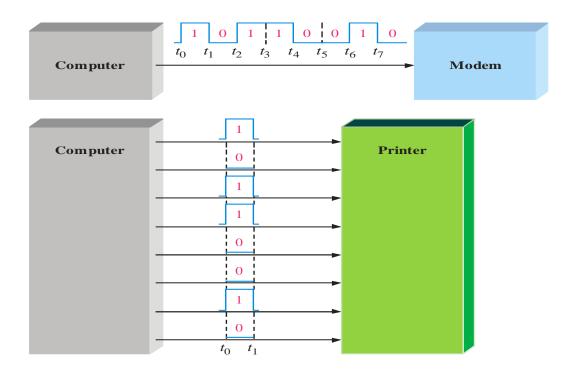
Parallel Transmission

- -each bit has it's own piece of wire along which it travels
- often used to send data to a printer

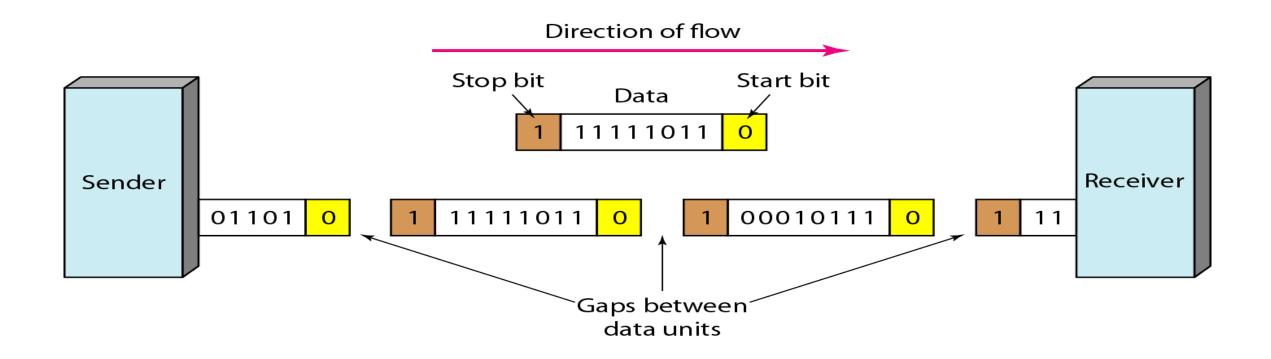


Serial and Parallel Data

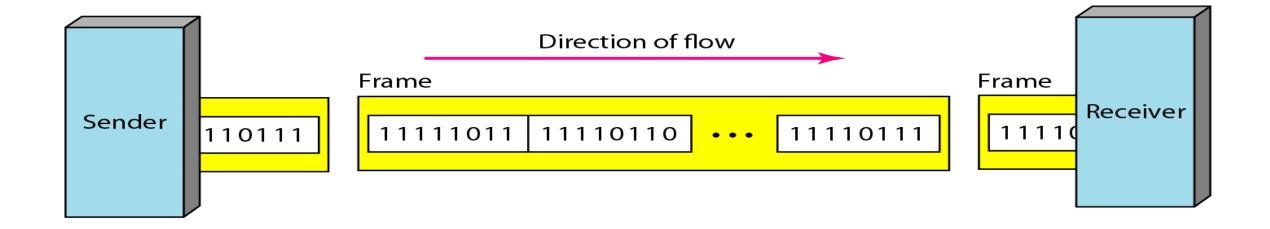
Data can be transmitted by either serial transfer or parallel transfer.



Asynchronous transmission



Synchronous transmission





Data

Symbols

- A symbol is a mark, sign, or word that indicates, signifies, or is understood as representing an idea, object, or relationship.
- Symbols allow people to go beyond what is known or seen by creating linkages between otherwise very different concepts and experiences.
- All communication (and data processing) is achieved through the use of symbols.
- Symbols take the form of words, sounds, gestures, ideas, or visual images and are used to convey other ideas and beliefs.
- For example, a red octagon is a common symbol for "STOP"; on maps, blue lines often represent rivers; and a red rose often symbolizes love and compassion.
- Numerals are symbols for numbers; letters of an alphabet may be symbols for certain phonemes; and personal names are symbols representing individuals.

Data – Information

- Data: Facts or pieces of information that have not gained meaning, have not been associated, have not been assimilated, and have not been processed. They are in forms devoid of any content. They carry no comments but are available for processing. Raw data.
- The computer takes data as input to process it and stores it in memories; processed and produced as output. The produced output is recorded in memory, displayed on the screen or transferred to other systems via I/O devices.
- Information: Giving meaning to data by adding value to it. It is the result of bringing together
 and arranging interrelated data for a certain purpose and has a meaning and news quality.
 From an institutional perspective, information is a database with meaning. Data is
 transformed into information by adding value through content processes. Information arises
 from data and information turns into knowledge.
- Information: In general, it emerges through the interpretation of data and information.
- Big Data: The concept of "Big Data" has emerged as data has increased greatly in terms of speed, diversity and capacity (volume) and technology has supported this increase and produced new solutions.

Data - Information - Knowledge - Wisdom

- Symbols: Numbers and symbols are pieces of information such as numbers, words, images, video and sound that are transferred to the computer's memory during the input phase.
- Signals: electrical, electromagnetic, akustic, gravity
- Data: Facts or pieces of information that have not gained meaning, have not been associated, have not been assimilated, and have not been processed. They are in forms devoid of any content. Sometimes it is a physical event, uninterpreted observations. They carry no comments but are available for processing. They are not effective in decision making.
- Information: What, who, when and where questions need to be answered. Information is processed, organized and meaningful data. Information is organized, meaningful and useful data. During the output phase, the information created is put into presentation form with printed reports, graphics and visuals. The information is stored on the computer for future use.
- Knowledge: Increasing performance in decision-making, estimation and searching for the truth.
- Understand: To become conscious by understanding, comprehending and feeling.
- Wisdom: It is evaluated understanding. It is about making decisions and interpreting by questioning and guessing.

Data Types

Symbols

Numbers: integer, float, complex, character, string, binary, boolean

Signals: Sound, heat, electricity, electromagnetic, smell, vibration,

picture

texts

Graphics

Tables

images

Transactions

Videos

- Data types are of three basic types: Numeric, Alphabetic, and Alphanumeric. Numeric Data consists of numbers only.
- Alphabetic Data consists of only letters and a space character, while alphanumeric data consists of symbols.

Data Quality

- Data quality issues:
 - Noise
 - Outliers (Aykırı değerler)
 - Wrong data
 - Fake data
 - Missing Values
 - Duplicate Data (Yinelenen veriler)
 - Similarity and Dissimilarity Measures (Benzerlik ve Farklılık Ölçüleri)

Data Science

- Veri Bilimi, bilgiler hakkında sonuçlar çıkarmak amacıyla istatistik ve makine öğrenimi tekniklerini kullanarak ham verileri analiz etme bilimidir.
- Data Science is the science of analyzing raw data using statistics and machine learning techniques to draw conclusions about the information.

Data Science is the science of analyzing raw data.

- Data gathering; Sensors, Telemetry systems, Internet, Data base management
- Data visualization
- Finding statistical measures by evaluating data
- Creating mathematical models and algorithms

Data Structures

- Lists
- Arrays
- Queue
- Trees
- Stacks
- Storage Hash structure



Numbers Systems

- Addition:
 - Add
 - Plus
 - Sum
 - Total
 - Increased by
 - More than

- Subtraction:
 - Minus
 - Difference
 - Subtract
 - Less than
 - Decreased by
 - less

- Multiplication:
 - Product
 - Times
 - multiply

- Division:
 - Quotient
 - divide

Add	Subtract	Multiply	Divide
Plus	Minus	Times	Divided by
The sum of	The difference of	The product of	The quotient of
Increased by	Decreased by	of	

Translating Verbal Phrases

- A. A number increased by 5
- B. 7 less than a number
- C. 3 more than twice a number
- D. 4 decreased by the quotient of a number and 7
- E. 16 increased by a number is 27
- F. The difference of twice a number and 3 equals -4
- G. The product of ½ and a number is 36
- H. -3 is equal to twice the sum of a number and 2

Numbers

Natural Numbers: Zero and any number obtained by repeatedly adding one to it.

Examples: 100, 0, 45645, 32

Negative Numbers: A value less than 0, with a – sign

Examples: -24, -1, -45645, -32

Integers: A natural number, a negative number, zero

Examples: 249, 0, - 45645, - 32

Rational Numbers: An integer or the quotient of two integers

Examples: -249, -1, 0, 3/7, -2/5

Representing Numbers

- Positive whole numbers
 - We already know one way to represent them: i.e., just use base 2 number system
- All integers, i.e., including negative integers
 - Set aside a bit for storing the sign
 - 1 for +, 0 for –
- Decimal numbers, e.g., 3.1415936, 100.34
 - Floating point representation:
 - sign * mantissa * 2 exp
 - 64 bits: one for sign, some for mantissa, some for exp.

Decimal Numbering System

Knowledge of different number systems and digital codes is quite useful when working with almost any type of digital computer. This is true because a basic requirement of these devices is to represent, store, and operate on numbers. In general, computer work on binary numbers in one form or another; these are used to represent various codes or quantities.

The decimal system, which is most common to us, has a base of 10. The radix or base of a number system determines the total number of different symbols or digits used by that system. For instance, in the decimal system, 10 unique numbers or digits—i.e., the digits 0 through 9—are used: the total number of symbols is the same as the base, and the symbol with the largest value is 1 less than the base.

The value of a decimal number depends on the digits that make up the number and the place value of each digit. A place (weight) value is assigned to each position that a digit would hold from right to left. In the decimal system the first position, starting from the rightmost position, is 0; the second is 1; the third is 2; and so on up to the last position. The weighted value of each position can be expressed as the base (10 in this case) raised to the power of the position. For the decimal system then, the position weights are 1, 10, 100, 1000, and so on. Figure 6.1 illustrates how the value of a decimal number can be calculated by multiplying each digit by the weight of its position and summing the results.

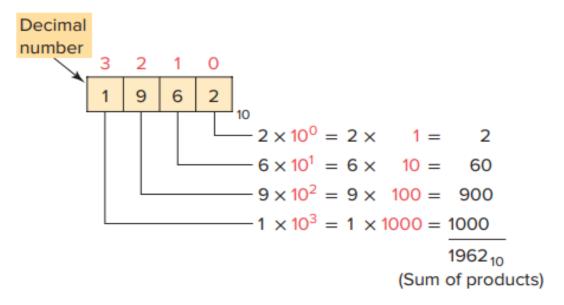


Figure 6.1 Weighted value in the decimal system.

Natural Numbers

How many ones are there in 642?

$$600 + 40 + 2$$
?

Or is it

384 + 32 + 2?

Or maybe...

1536 + 64 + 2?

642 is 600 + 40 + 2 in BASE 10

The base of a number determines the number of digits and the value of digit positions

Positional Notation

Continuing with our example...

642 in base 10 positional notation is:

$$6 \times 10^{2} = 6 \times 100 = 600$$

+ $4 \times 10^{1} = 4 \times 10 = 40$
+ $2 \times 10^{0} = 2 \times 1 = 2 = 642$ in base 10

This number is in base 10

The power indicates the position of the number

Positional Notation

Example:

642 is
$$6 * 10^2 + 4 * 10 + 2$$

As a formula:

R is the base of the number

$$d_{n} * R^{n-1} + d_{n-1} * R^{n-2} + ... + d_{2} * R + d_{1}$$

n is the number of digits in the number

d is the digit in the ith position in the number

The Number System

When learning about 'data representation' we understand the importance and versatility of binary numbers (İkili sayıların önemi ve çok yönlülüğü) and how binary is used to store data in computer systems.

- Numbers
- Text
- Images
- Sound
- Instructions
- ...are all stored in binary and we will understand how this is done!

It is fairly easy to understand how numbers are stored in binary format in computer systems. But what about text, images and sound? The key thing to remember is that text, images and sound

Types of number

- Number types are used to define the type of a variable. It defines what type of numbers we are going to store in a variable. The data stored in memory as binary numbering (1/0: bit) can be of many types. For example, a person's age is stored as a numeric value and his or her address is stored as alphanumeric characters.
- The decimal, binary, octal, and hexadecimal numbering systems and be able to convert from one numbering or coding system to another. The terms bit, byte, word, least significant bit (LSB), and most significant bit (MSB) as they apply to binary memory locations.
 - Numeric int, float, complex
 - String str
 - Sequence list, tuple, range
 - Binary bytes, byte array, memoryview
 - Mapping dict
 - Boolean bool
 - Set set, frozenset
 - None NoneType

Data Representations

• Sizes (in Bytes)

Data Type	Compaq Alpha	Typical 32-k	oit Intel L	A32
• int	4	4	4	
long int	8	4	4	
• char	1	1	1	
short	2	2	2	
float	4	4	4	
double	8	8	8	
 long double 	8	8 1	.0/12	
• char *	8	4	4	

- Numbering systems
 - Decimal
 - Binary (İki sayı sistemi 0/1)
 - Bits: 0 ya da 1
 - Bytes: 8bit
 - Hexadecimal: 4bit
 - Numbers conversion among different systems
- The on and off states of the capacitors in RAM can be thought of as the values 1 and 0, respectively.
- Therefore, thinking about how information is stored in RAM requires knowledge of the **binary (base 2) number system.**

The Decimal Number System

- The decimal number system is also known as **base 10**. The values of the positions are calculated by taking 10 to some power.
- Why is the base 10 for decimal numbers?
 - Because we use 10 digits, the digits 0 through 9.
- The decimal number system is a positional number system.
- Example:

5 6 2 1
$$1 \times 10^{0} = 1$$

 $10^{3} \cdot 10^{2} \cdot 10^{1} \cdot 10^{0}$ $2 \times 10^{1} = 20$
 $6 \times 10^{2} = 600$
 $5 \times 10^{3} = 5000$

Decimal Numbering System

- Ten symbols: 0, 1, 2, 3, 4, 5, 6, 7, 8, 9
- Represent larger numbers as a sequence of digits
- Each digit is one of the available symbols
- Example: 7061 in decimal (base 10)
- $(7061)_{10} = (7 \times 10^{3}) + (0 \times 10^{2}) + (6 \times 10^{1}) + (1 \times 10^{0})$

Number-Base Conversion

Name	Radix	Digits
Binary	2	0,1
Octal	8	0,1,2,3,4,5,6,7
Decimal	10	0,1,2,3,4,5,6,7,8,9
Hexadecimal	16	0,1,2,3,4,5,6,7,8,9,A,B,C,D,E,F

The six letters A, B, C, D, E, and F in hexadecimal represent: 10, 11, 12, 13, 14, and 15, respectively.

Numbering Systems

Decimal is base 10 and has 10 digits:

0,1,2,3,4,5,6,7,8,9

Binary is base 2 and has 2 digits:

0,1
For a number to exist in a given base, it can only contain the digits in that base, which range from 0 up to (but not including) the base.

What bases can these numbers be in? 122, 198, 178

Binary Numbering System

- The decimal number system consists of symbols 0 through 9. It is multiplied by 10 to create a two-digit decimal number system. It is multiplied by 100 to create a three-digit number system. The steps are continued in multiples of 10.
- The binary number system consists of 0 and 1. It is expressed by the 0 or 1 output of the transistor. It exists as an electrical signal. Digits are expressed as multiples of 2.
- Example: (10^9)10=1*10^2+0*10^1+9*10^0
- Example: (10^1)2=1*2^2+0*2^1+1*2^0=(5)10
- In the computer, everything is kept as 1 or 0.
- (100 0001)b is the symbol, which corresponds to the value 65 in the decimal number system, or the character A.
- In the binary world, everything can be expressed as 1 or 0. Its equivalent in computer memory is called a bit.
- Bits come together to identify more bits. For example, in a 2-bit system, four different states or symbols 00, 01,10,10 can be created. When it is desired to be displayed numerically, it can be expressed as 0, 1, 2, 3.

Algebraic Expressions

Key Vocabulary

Expression – a math sentence *without* equal signs

Equation – a math sentence *with* equal signs

<u>Variable</u> – a letter that is used to represent a number

Terms – the part of an expression that is being added together

<u>Coefficient</u> – the number part of the term that has a variable with it

Constant Term – a term that has a number but no variable

Like Terms – terms that have identical variables

Inverse Operation – the opposite operation used to solve an equation

Expressions vs Equations

Expressions – written as phrases

Example – the sum of six and a number x + 6

<u>Equations</u> – written as sentences

Example – the sum of six and a number *IS* ten x + 6 = 10

What is the difference between a numeric expression and an algebraic or variable expression?

Numeric Expression

$$-3 + 2 + 4 - 5$$

Algebraic Expression

$$-3x + 2y - 4z - 5$$

An algebraic or variable expression consists of three parts

- Variable
- Coefficient
- Constant

In the expression 12 + B, the letter "B" is a variable.

The <u>variable</u> is a symbol or letter that represents a number. What are the variables in the expression below?

$$f(x,y,z)=-4x + 3y - 8z + 9$$

x,y,z: Independent variable

f(x,y,z): Dependent variable

What are coefficients?

A **coefficient** is the number multiplied by the variable in an algebraic expression.

Algebraic Expression	<u>Coefficient</u>
6m + 5	6
8r + 7m + 4	8, 7
14b - 8	14

The <u>coefficient</u> is the number that multiplies the variable. More plainly, it is the number in front of a variable.

What are the coefficients in the expression below?

$$f(x,y,z)=-4x + 3y - 8z + 9$$

 $f(x,y,z)=ax + by + cz + d$

What is a term?

A **term** is the name given to a number, a variable, or a number and a variable combined by multiplication or division.

Algebraic Expressions

<u>Terms</u>

a + 2

a, 2

3m + 6n - 6

3m, 6n, - 6

The **constant** is any term that does not have a variable.

What is the constant in the expression below?

$$f(x,y)=-8 + 5y + 3x$$

What are constants?

A constant is a number that cannot change its value.

```
In the expression: 5x + 7y - 2 the constant is - 2.
```

An algebraic expression can also be classified as a polynomial which is an expression that consists of more than one term. Two types of polynomials are **binomials and trinomials**.

A binomial has two terms. Ex: 3x + 4

A trinomial has three terms. Ex: $4a^2 + 3a + 7$

Evaluating expressions examples

Example 1

Evaluate 4y - 15 for y = -9

- 4y 15
- 4(-9) 15
- -36 15 = -51

Example 2

Evaluate $3ab + c^2$ for a = 2, b = -10, and c = 5.

- $3ab + c^2$
- $3(2)(-10) + 5^2$
- -60 + 25 =**-45**

Example 3

Evaluate 6(g + h) for g=8 and h = 7.

- 6(8 + 7)
- 6 (15) = **90**

İkili sayı sisteminde değişkenler ve katsayılar

 İkili sayı sisteminde değişkenler ve katsayılar sadece 1 ya da 0 değeri alırlar.



Binary Numbering System Bit (0/1)

Data Representation in Computer

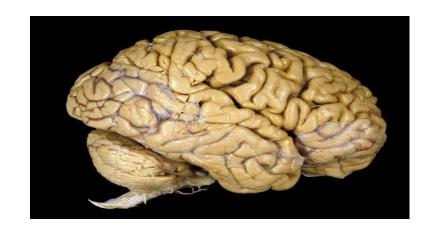
- In all computers, all information is represented by using binary numbering system (bit: 0/1).
- Each storage location (cell Transistor): has two states
 - low-voltage electrical signal => 0
 - High-voltage electrical signal => 1
 - it can store a binary digit, bit
- Eight bits grouped together to form a byte
- Two bytes grouped together to form a word
 - Data bus length of a computer, e.g., 8bits computers, 16bits computers, 32 bits computer, 64 bits computer, 128 bits. Data bus length of processor is 8, 16, 32, 64 or 128

Why Binary Arithmetic?

- All data is recorded as 1 or 0 in the computer's memory.
- All operations in the processor are done with 1s and 0s.
- he hardware is made with electrical signals only in the binary number system of 1 and 0.
- Must represent all numbers, integers or floating point, positive or negative, by binary digits, called bits.
- Can devise electronic circuits to perform arithmetic operations: add, subtract, multiply and divide, and logical operations, comparisons on binary numbers.

Why Binary Arithmetic?

$$3 + 5$$



= 8

$$0011 + 0101$$



= 1000

Binary Number System

- Computers use the binary number system, which consists of only the digits 0 and 1.
- 1 represents presence, 0 represents absence. 1 means there is voltage (5Volts), 0 means there is 0 voltage.
- Symbols (All numbers, alphabets), text, picture, video, signals represent in the binary system consist of 1 and 0 inside the computer.
 - Numbers (positive, negative, integer, float, fraction), strings, booleans, images, sounds, programming instructions represent as bits.
 - For unsigned integer values, we can store them directly using binary. The numbers we use in our daily lives are in base ten, also known as decimal.
 - As we know, the numbers that make up the decimal system are 0, 1, 2, 3, 4, 5, 6, 7, 8, 9.
- In computer systems we focus on the binary number system (base 2), Why? Because the digital components that make up the computer can be in one of two states: on or off.
- The bit name binary digit is derived from the binary number system.
- While the numbers and letters typed on the keyboard are translated into a form that the computer can understand, the binary number system comes into play.

Basic Units of Digital systems

- The basic unit of information in computer systems is bit: (1/0)
- Bit: 0/1; bits are represented by electrical signals. Electronic circuit element Transistor. Data Bus, Memory compartment contents, Registers
- Byte: Represents 8 bits of data. Or it points to the 1 byte memory slot. It represents base-2 operations in memory. Address Bus; memory and memory choose the eye.
- Bit/sec: Represents the amount of data to be transferred or processed per second. It is represented by exponential operations in base 10.
- Qubit: Represents the smallest data in quantum caomputers. Qubits are represented by electrons.

Digital Data (Binary numbering system)

Types of data

- Text: ASCII code, unicode
- Numbers: Integers, Reals, Floating point numbers, Fractional number, binary, ...
- Binary Number systems: Ondalıklı sayı sistemi (Decimal) aşağıdaki sayı sistemine dönüştürülür.
 - Binary (İki sayı sistemi 0/1)
 - Bits: 0 ya da 1
 - Bytes: 8bit
 - Hexadecimal: 4bit
 - Octal

Numbers

- Binary number representation of integers
- If we save one bit to signify positive (+) or negative (-), then an n-bit binary word can represent integers in the range: $-2^{(n-1)}-1..+2^{(n-1)}$
- ASCII code (American Standard Committee on Information Interchange)
 A unique 8-bit binary code for each character:
 - A-Z, a-z, 1-9, .,¬!"£\$\$%^&*() +
 - Special unprintable characters such as the
 - ENTER key (CR for carriage return)

Binary Signals- Bit (0/1)

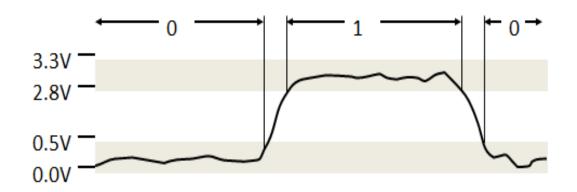
Binary signal, binary state signal: Two-state data (0/1).

- off & on
- It is carried and stored by electrical signals.

low voltage & high voltage; 0v & 5v

Bit: It is not only a mathematical concept, but also has its counterpart in the physical world.

- The binary number system has the value 0 or 1 and nothing else.
- A bit is the smallest unit of information in a computer





- Bit is the basic concept, the cornerstone of information used in computer systems.
 Bits consist of 0s or 1s. They are mathematical objects, and they correspond to physical situations.
- A bit (0/1) is the basic unit of information. Bits are used to represent information in computers. Regardless of its physical implementation, a bit is always understood to be either a 0 or a 1. An analogy to this is a light switch with 0 representing the off position and 1 representing the on position.
- In normal or "classical" computing, the basic unit of information is the bit. A bit can be in one of two states, 0 or 1.
- The building block of classical computing devices is represented by the two-state system (0/1).
- In fact, any system that has a finite set of discrete, steady states with controlled transitions between them will do.

Bit

- The values a bit can take are 0 or 1. Number of states=2^1=2, State: 0.1
- If we have two bits of information, how many states are there? There are 2^2= 4 situations. Status: 00, 01, 10,11.
- There are 8 states that three bits can take: 000, 001, 010, 011, 100, 101, 110, 111. Number of states=2^3=8
- The number of states that n bits can take = 2^n. It is defined as a state space.

For example, the temperature of the room is 25 degrees, this is information.

- (25)d=2^4+^2^3+2^0; Indexing = 43210
- (25)d=(11001)b, [(25)]_10=[(11001)]_2
- How to convert a binary number to decimal? It is indexed starting with 0 from the right. Index values from 1 to 2 are added together. ((11001))_2=2^4+2^3+2^0=25.
- (11001)b: this is information stored in the computer. It represents data in the binary number system.
- In the computer, all physical systems and signals are represented by bits.

Bit (0/1)

- BIT is a unit of information equivalent to the result of a choice between only 2 possible alternatives in the binary number system.
- Bits consist of 0s or 1s. They are mathematical objects and correspond to physical situations.
- It is information that is asked to a system and is one of two answers given as true or false.
- Bit is the basic concept, the cornerstone of information used in computer systems.
- Bits are used to represent information by computers.
- Regardless of its physical implementation, a bit is always understood to be 0 or 1.
- An analogy to this is a light switch with 0 representing the off position and 1 representing the on position.
- There are two types of bits, a classical cbit, bit (0,1) and a quantum bit, qubit (|0) , |0)
).

Bit

Bit: In digital electronics and the binary number system, there are only values 0 and 1. All operations are performed on these two values. Each piece of information 0 or 1 is called a bit. Information consisting of bit \rightarrow 0/1

- Bits are the units used to describe an amount of data in a computer systems.
 - -1 kilobit (Kbit) $= 1 \times 10^3$ bits = 1,000 bits
 - $1 \text{ megabit (Mbit)} = 1 \times 10^6 \text{ bits} = 1,000,000 \text{ bits}$
 - -1 gigabit (Gbit) = 1 x 10⁹ bits = 1,000,000,000 bits

Bit/Sec

Bit/Second: Bit/sec→Serial bits (Data) are transmitted from one point to another. Or it is the bit, that is, the amount of information processed in one second. BPS (Bit Per Second); The number of bits transmitted per second is called bps.

- Seconds are the units used to measure time
 - 1 millisecond (msec) = 1×10^{-3} seconds = 0.001 seconds
 - -1 microsecond (msec) = 1×10^{-6} seconds = 0.000001 seconds
 - -1 nanosecond (nsec) = 1×10^{-9} seconds = 0.000000001 seconds
- Bits per second are the units used to measure channel capacity/bandwidth and throughput
 - Bit per second (Bps)
 - Kilobits per second (Kbps)
 - Megabits per second (Mbps)

Calculating Memory Capacity

- The bit grouping created by the address lines of CPU selects the memory, memory slot and I/O unit by using address lines. If the number of address lines is n bits, the memory capacity is 2ⁿ bytes.
- How many bytes in 64kbytes? 64*2^10 bytes=2^6 * 2^10=2^16 bytes=2^n. Here n=16 is number of the address lines of the memory.
- Then, if the number of address lines is 19, how much bytes is the memory capacity? How many Kbytes is it?2^19 bytes=2^9Kbytes=512Kbytes
- If the memory capacity is 128Kbytes, what is the number of address lines? 128Kbyte=(2^7)*(2^10)=2^17 bytes, number of address lines=17.
- The memory capacity is calculated by an enginner and its value is 397Gbytes, what is the number of address lines? We don't use 397, because we are looking for 2^n. So we take 512 (2^9) instead of 397. Why? Because nearst and greater than 397. 512Gbyte = (2^9)*(2^30) = 2^39 bytes. Number of address lines =39.

Question: How many address lines? 16 pieces. From where? Number of bit groupings, n=16

Description: Since it defines the memory capacity of 64 Kbytes, there are 16 address bus lines. 2^16=2+6 *
 2^10=64Kbytes

Bits and Bytes are Slightly Different

"Kilo" or "Mega" have slightly different values when used with bits per second or with bytes.

When Referring to Bytes (as in computer memory capacity)

```
- <u>Kilo</u>byte (KB) 2^{10} = 1,024 bytes
```

$$-$$
 Megabyte (MB) $2^{20} = 1,048,576$ bytes

$$-$$
 Gigabyte (GB) $2^{30} = 1,073,741,824$ bytes

$$-$$
 Terabyte (TB) $2^{40} = 1,099,511,627,776$ bytes

- When Referring to Bits Per Second (as in transmission rates): It is the data processing or data transfer rate.
 - <u>Kilo</u>bit per second (Kbps) = 1000 bps (thousand)
 - Megabit per second (Mbps) = 1,000,000 bps (million)
 - Gigabit per second (Gbps) = 1,000,000,000 bps (billion)
 - <u>Tera</u>bit per second (Tbps) = 1,000,000,000,000 bps (trillion)

Byte

Byte: Gives the memory size; also represent 8bits data. In electronics and computer science, it is a memory measurement unit that generally incorporates 1 or 0 values along an 8-bit sequence and is independent of the type of information recorded.

The term bit is defined as the smallest unit of memory that marks or describes an 8-bit value. Byte→memory defines the 8-bit address box or memory size.

- Kilobyte (K) $2^{10} = 1,024$ bytes
- Megabyte (M) $2^{20} = 1,048,576$ bytes
- Gigabyte (G) $2^{30} = 1,073,741,824$ bytes
- Terabytes (T) $2^{40} = 1,099,511,627,776$ bytes
- Petabytes (P) $2^{50} = 1,125,899,906,842,624$ bytes
- Exabytes (E) $2^{60} = 1,152,921,504,606,846,976$ bytes
- Zettabytes (Z) $2^{70} = 1,180,591,620,717,411,303,424$ bytes
- Yottabytes (Y) $2^{80} = 1,208,925,819,614,629,174,706,176$ bytes

Examples

How many Bytes is 12Gbyte?

- İnstead 12 we take 16 alınır. (2ⁿ olmalıdır.)
- $16GByte=2^4 2^{30} = 2^{34} Byte$

How much Bytes is 16Gbyte?

How much Bytes is 128Mbyte?

• $128MByte=2^7 2^{20} = 2^{27} Byte$

How much Bytes is 256Mbyte?

• $256MByte=2^8 2^{20} = 2^{28} Byte$

How much Bytes is 4Kbyte?

• $4KByte=2^2 2^{10} = 2^{12} Byte$

How much Bytes is 32Tbyte?

- $32TByte=2^5 2^{40} = 2^{45} Byte$
- $32TByte=2^5 2^{40} = 2^{45} / 2^{10} = 2^{35} KByte$
- $32TByte=2^5 2^{40} = 2^{45} / 2^{20} = 2^{25} MByte$
- $32TByte=2^5 2^{40} = 2^{45} / 2^{30} = 2^{15} GByte$
- $32TByte=2^5 2^{40} = 2^{45} / 2^{40} = 2^5 TByte$

How much Bytes is 8Pbyte?

• 8PByte= $2^3 2^{50} = 2^{53}$ Byte

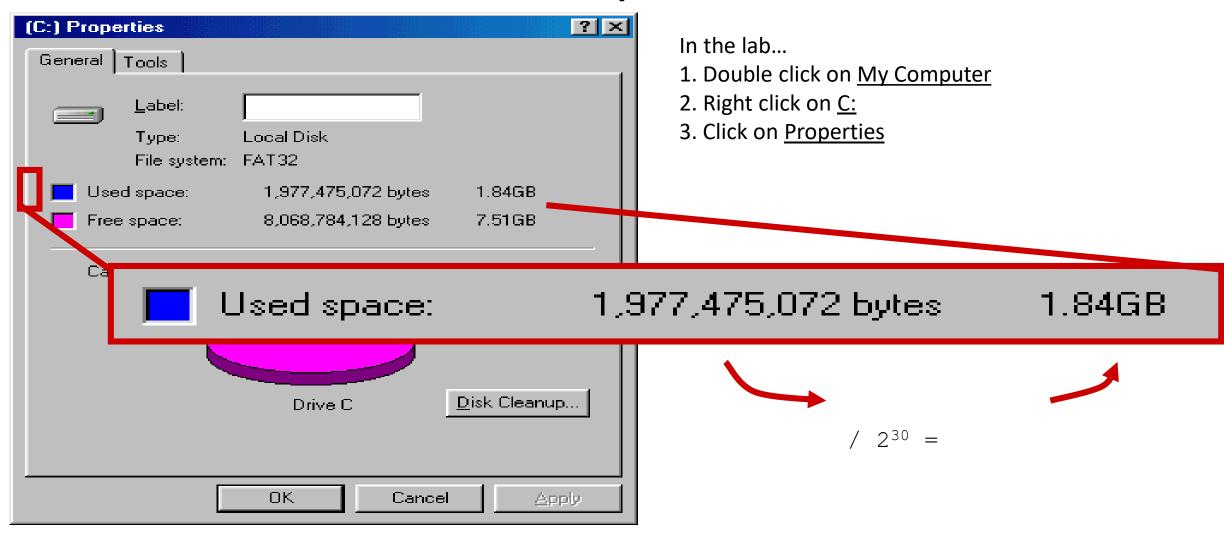
Baud Rate

Baud Rate is the unit for symbol rate or <u>modulation</u> rate in **symbols per second** or **pulses per second**.

Example: Let the transmission speed of a data transmission line be 4800 baud/sec. If this transmission contains information encoded with 4 bits per baud (symbol), our speed in bps is 4800 * 4 = 19200 bps. The purpose of using Baud Rate is to use bandwidth more efficiently.

- The symbol duration time T_s can be calculated as: Ts=1/fs,where f_s is the symbol rate.
- Example: Communication at the baud rate 1000 Bd means communication by means of sending 1000 symbols per second. The symbol duration time is 1/1000 second (that is, 1 millisecond). In digital systems with binary code, 1 Bd = 1 bit/s. By contrast, non-digital (or analog) systems use a continuous range of values to represent information and in these systems the exact informational size of 1 Baud varies.

Example





Data Representation in Computer

Bit processing

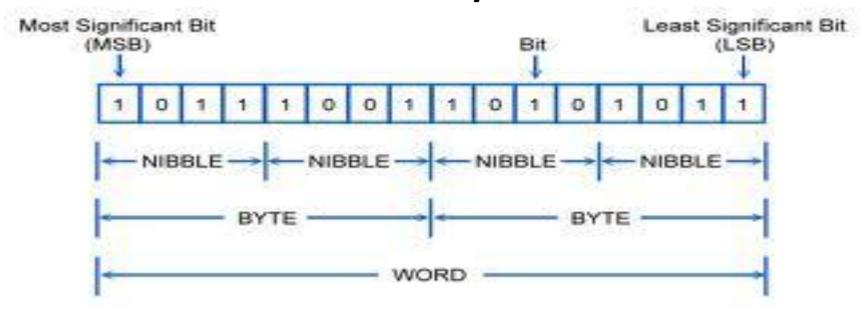
- Data types: decimal, integer, floating, complex, binary, boolean, hex
- Digital numbering system: bit (1/0), byte (8 bit), word (16 bit), double word (32 bit), quad word (64 bit), double quad word (128 bit), ten byte (80 bit)
- Converting binary number system to decimal or hex number system
- Addition and Shift
- Logic circuits, Boolean Algebra
- Comparison: <,≤, >, ≥, ≠, =
- Data transfer: bit/s
- Data processing: bit/s
- Data storage (memory): byte (2ⁿ byte; n: number of the address bus lines)
- Memory and memory slot selection (address bus lines are coming out of CPU)
- Data bus: Number of parallel lines (bytes) written or read to memory in 1 plock period;
 8bit, 16bit, 32bit, 64bit, 128bit, ...

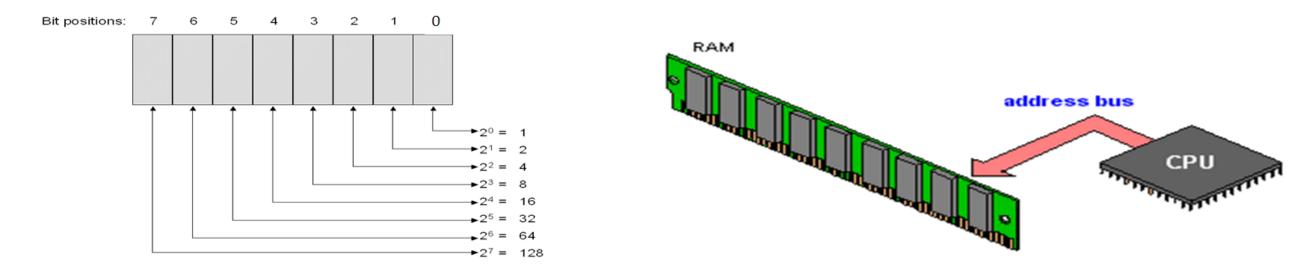
In binary numbering system Data Types and Size

- A bit is a single binary digit (a 1 or 0).
- A **byte** is 8 bits
- A word is 16 bits or 2 bytes
- Double word is 32 bits or 4 bytes
- Long word = 8 bytes = 64 bits
- Quad word = 16 bytes = 128 bits
- Programming languages use these standard number of bits when organizing data storage and access.
- What do you call 4 bits? (hint: it is a small byte) (Nibble)

Question: 10^9 bit/sec (Data processing or data transfer speed)

Bits and Bytes

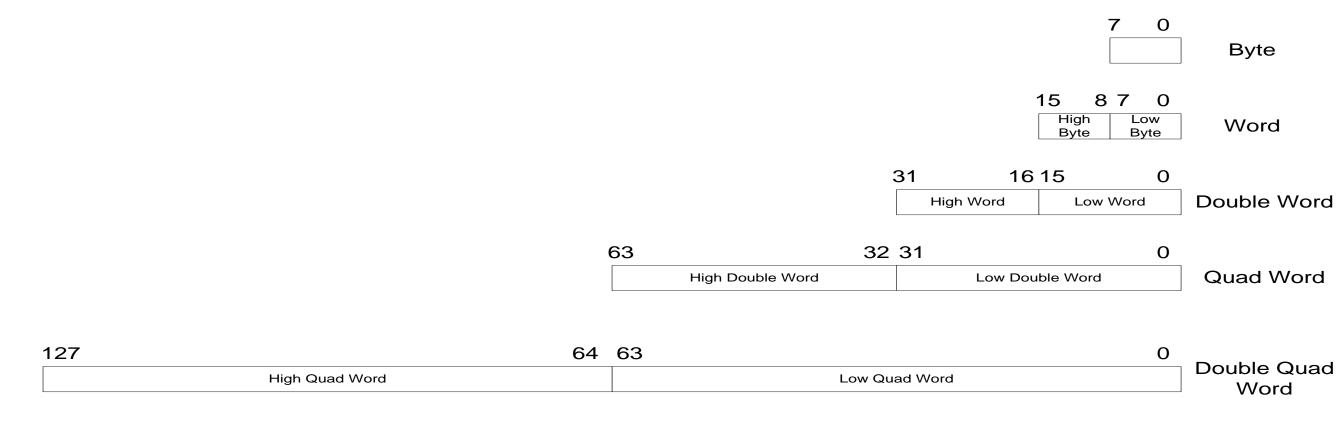




DATA SIZE

Nibble	4 bit	Nibble = 4 bit (n= 0-3) Range: 0-15
Byte	8 bit	Byte = 8 bit (n = 0-7) Range: 0 -255 Sign bit 7 Upper 4 3 Lower Nibble Nibble
Word	16 bit	Word = 16 bit (n= 0-15) Range: 0 -65,535 Sign bit 15 Upper byte 8 7 Lower byte 0
Long word	32 bit	Sign bit 31 Upper word 16 15 Lower word 0 MSB (Most significant Bit) LSB (Range: 0 -4,294,967,295 (Least significant Bit)

Data Types - size



Binary Numbering System

Binary System

The binary system uses the number 2 as the base. The only allowable digits are 0 and 1. With digital circuits it is easy to distinguish between two voltage levels (i.e., +5 V and 0 V), which can be related to the binary digits 1 and 0 (Figure 6.2). Therefore, the binary system can be applied quite easily to computer systems. Since the binary system uses only two digits, each position of a binary number can go through only two changes, and then a 1 is carried to the immediate left position

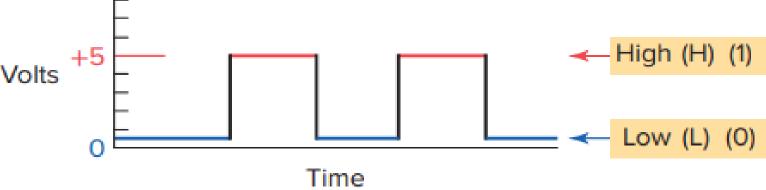


Figure 6.2 Digital signal waveform.

Binary Numbering System

- Binary is base 2
- Symbols: 0, 1
- Convention: (2)10 = (10)2 = (10)b
- What is (110)b in base 10?
- $(110)b = (110)2 = (1 \times 2^2) + (1 \times 2^1) + (0 \times 1^0) = (6)10$

Base 10	Base 2
0	0
1	1
2	10
3	11
4	100
5	101
6	110
7	111
8	1000
9	1001

Binary number system

- All computers use the binary system :
 - Binary number system: Base = 2. Thus there are 2 numbers: 0 and 1.
 - A single binary number is called a Binary digIT, or bit.
- Computers perform operations on binary number groups called bytes.
- Today, most computers use 32- or 64- bit :
- Bytes are subdivided into 8-bit groups called bytes.
- One-half a byte is sometimes referred to as a nibble (a term not often used anymore).

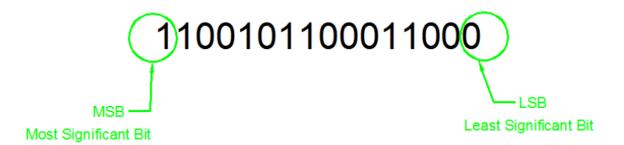
16 bitten yani 2 bayttan oluşan sayılara 1 word adı verilir.

1100101100011000

8 bitten oluşan sayılara

1 byte adı verilir.

Bir binary sayının en solundaki bit MSB, en sağındaki bit de LSB olarak isimlendirilir.



The Binary Number System

- The binary number system is also known as **base 2**. The values of the positions are calculated by taking 2 to some power.
- Why is the base 2 for binary numbers?
 - Because we use 2 digits, the digits 0 and 1.
- The binary number system is also a positional numbering system.
- Instead of using ten digits, 0 9, the binary system uses only two digits, 0 and 1.
- Example of a binary number and the values of the positions:



Figure 3 illustrates how the binary number 10101101 is converted to its decimal equivalent: 173.

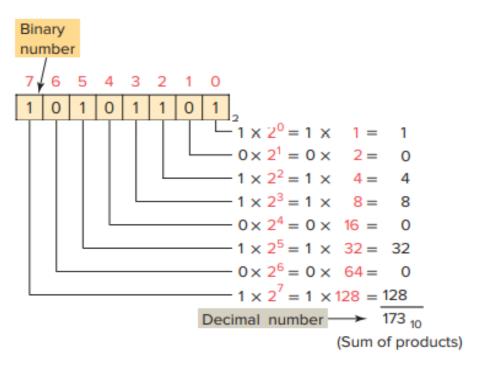


Figure 6.3 Converting a binary number to a decimal number.

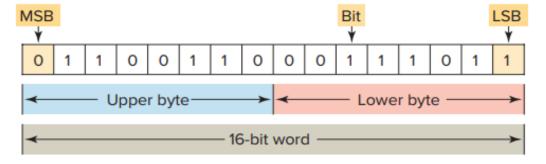


Figure 6.4 A 16-bit word.

Each digit of a binary number is known as a bit. In a processor-memory element consists of hundreds or thousands of locations. These locations, or registers, are referred to as words. Each word is capable of storing data in the form of binary digits, or bits. Bits can also be grouped within a word into bytes. A group of 8 bits is a byte, and a group of 2 or more bytes is a word. Figure 4 illustrates a 16-bit word made up of 2 bytes. The least significant bit (LSB) is the digit that represents the smallest value, and the most significant bit (MSB) is the digit that represents the largest value. A bit within the word can exist only in two states: a logical 1 (or ON)

condition, or a logical 0 (or OFF) condition.

To convert a decimal number to its binary equivalent, we must perform a series of divisions by 2. Figure 5 illustrates the conversion of the decimal number 47 to binary. We start by dividing the decimal number by 2.

Decimal number

If there is a remainder, it is placed in the LSB of the binary number. If there is no remainder, a 0 is placed in the LSB. The result of the division is brought down and the process is repeated until the result of successive divisions has been reduced to 0.

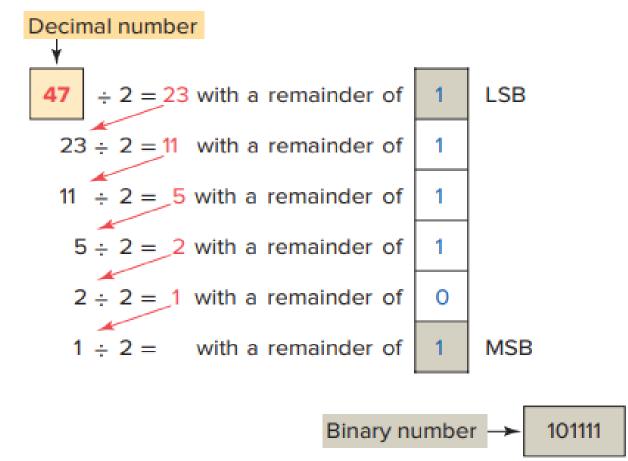
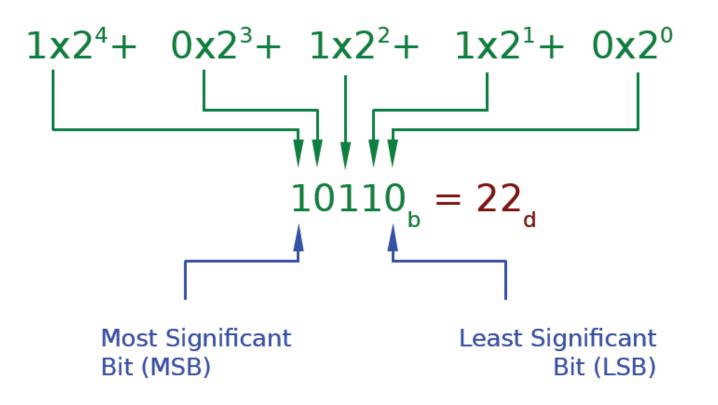


Figure 5.5 Converting a decimal number to a binary number.

Binary

Binary is exactly the same, only instead of ten digits/states (0 to 9) we have just two, so the base becomes 2:

Bilgisayar sistemlerinde 2 üzeri indeksleme 0,1,2,3,.. Biçimindedir. İndeksleme sağdan başlar.



Converting from Binary to Decimal

Converting From Decimal to Binary

- Make a list of the binary place values up to the number being converted.
- Perform successive divisions by 2, placing the remainder of 0 or 1 in each of the positions from right to left.
- Continue until the quotient is zero.
- Example: 42₁₀

$$2^{5}$$
 2^{4} 2^{3} 2^{2} 2^{1} 2^{0} 32 16 8 4 2 1 1 0 1 0 1 0

Binary Number Examples

$$- 11 = 1 \times 2^{0} + 1 \times 2^{1} = 3_{10}$$

-
$$101 = 1 \times 2^2 + 0 \times 2^1 + 1 \times 2^0 = 4 + 1 = 5_{10}$$
.

-
$$1001 = 1 \times 2^3 + 1 \times 2^0 = 8 + 1 = 9_{10}$$
.

$$- 1100 = 1 \times 2^3 + 1 \times 2^2 = 8 + 4 = 12_{10}.$$

-
$$11101 = 1 \times 2^4 + 1 \times 2^3 + 1 \times 2^2 + 1 \times 2^0 = 16 + 8 + 4 + 1 = 29_{10}$$
.

-
$$0.1 = 1 \times 2^{-1} = \frac{1}{2} = 0.5_{10}$$

-
$$0.111 = 1 \times 2^{-1} + 1 \times 2^{-2} + 1 \times 2^{-3} = 0.5 + 0.25 + 0.125 = 0.875_{10}$$

-
$$0.10001 = 1 \times 2^{-1} + 1 \times 2^{-5} = 0.5 + 0.03125 = 0.53125_{10}$$

-
$$1101.01 = 1 \times 2^3 + 1 \times 2^2 + 1 \times 2^0 + 1 \times 2^{-2} = 8 + 4 + 1 + 0.25 = 13.25_{10}$$

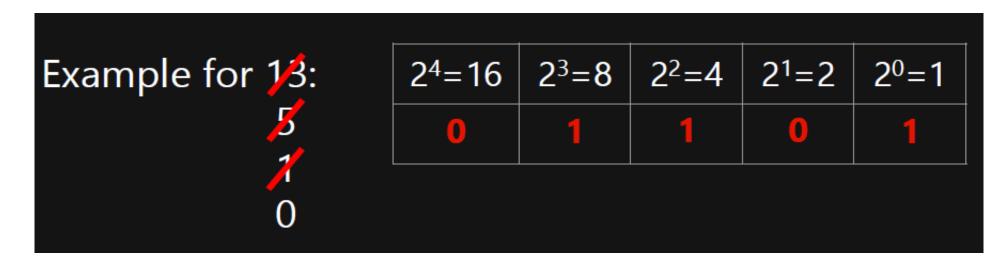
-
$$11.001 = 1 \times 2^{1} + 1 \times 2^{0} + 1 \times 2^{-3} = 2 + 1 + 0.125 = 3.125 \times 1 \times 2_{10}$$

-
$$10.0011 = 1 \times 2^{1} + 1 \times 2^{-3} + 1 \times 2^{-4} = 2 + 0.125 + 0.0625 = 2.1875_{10}$$

Converting from Decimal to Binary

Given a decimal number N:

- List increasing powers of 2 from right to left until ≥ N
- From left to right, ask is that (power of 2) ≤ N?
 - If YES, put a 1 below and subtract that power from N
 - If NO, put a 0 below and keep going



- A 16-bit binary number
- 15 14 13 12 11 10 9 8 7 6 5 4 3 2 1 0
- = $1 \times 2^{8} + 1 \times 2^{7} + 1 \times 2^{4} + 1 \times 2^{3} + 1 \times 2^{2} + 1 \times 2^{4} +$
- \bullet = 256 + 128 + 16 + 8 + 4 + 2 + 1
- = 415

Binary'den decimal'a çevirme örnekleri

• Örnek:

- (1010)2 = (?)10
- $(1010)2 = 1x2^3 + 0 \times 2^2 + 1 \times 2^1 \times 0x2^0$
- (1010)2 = 8 + 0 + 2 + 0
- (1010)2 = 10

• Örnek:

- (11001)2 = (?)10
- $(11001)2 = 1x2^4 + 1x2^3 + 0 \times 2^2 + 0x2^1 + 1x2^0$
- (11001)2 = 16 + 8 + 0 + 0 + 1
- (11001)2 = 25

Negative decimal numbers represent as binary numbering system

- If we let the most significant bit (MSB) signify positive or negative numbers (1 for negative; 0 for positive) Word olara tanımlayalım (16 bit)
- Then
- +9 = 000000000001001
- -9 = 100000000001001
- +9 + (-9) = 1000000000010010
- The result is NOT zero. This is a problem!

- So we need a different representation for negative numbers
- Called 2s-complement
- Take the 1s-complement of the positive number:
- (+9)d: 0 0 0 0 0 0 0 0 0 0 1 0 0 1
- 1'ler 0; 0'lar 1 yapılır:
- 1111 1111 1111 0110
- Note that the addition of the 1s-complement and the original number is not zero. +1 eklenir.
- To get the 2s-complement, add 1
- 1111111111110110+1
- _____
- 1111111111110111
- Now do the addition:
- 0000000000001001+
- 11111111111110111
- •
- 0000000000000000

- Another example:
- +1 + (-1)
- 000000000000001+
- 111111111111111
- 000000000000000

Örnek: (16bit)

- (-27)d
- (+27)d=16+8+2+1=2^4+2^3+2^1+2^0
- İndis: 15 14 13 12 11 10 9 8 7 6 5 4 3 2 1 0
- 0 0 0 0 0 0 0 0 0 0 1 1 0 1 1
- (+27)d=0000 0000 0001 1011 =(001B)h
- 1111 1111 1110 0100 (1'ler 0; 0'lar 1 yapıldı)
- 1111 1111 1110 0100
- 1
- 1111 1111 1110 0101=(-27)d

Binary Sayıların Decimal Sayılara Dönüştürülmesi:

- $(100011)_2$ = (?)h indis: 5,4,3,2,1,0 1 olanların indis karşılığı= 2^indis $2^5 + 2^1 + 2^0 = 32 + 2 + 1 = (35)_{10} = (23)$ h
- Ondalıklı Binary Sayıların Decimal Sayılara Dönüştürülmesi: $(111,101)_2 = 2^2 + 2^1 + 2^0 + 2^{-1} + 2^{-3} = 4 + 2 + 1 + 1/2 + 1/8 = 7,625$
- Decimal Sayıların Binary Sayılara Çevrilmesi: $(172)_{10} = (128+32+8+4)_{10} = (2^7+2^5+2^3+2^2)_{10} = (1010\ 1100)_2 = (AC)_{16}$
- Ondalıklı Decimal Sayıların Binary Sayılara Dönüştürülmesi
- $(10,75)_{10}$ =? $(10)_{10}$ = $(2^3+2^1)_{10}$ = $(1010)_2$, 2^{-1} =1/2=0,5 2^{-2} =1/4=0,25, $(10,75)_{10}$ = $(1010,11)_2$

From Base 10 to Base 2: using table

- Input: a decimal number
- Output: the equivalent number in base 2
- Procedure:
 - Write a table as follows
 - 1. Find the largest two's power that is smaller than the number
 - 1. Decimal number 234 => largest two's power is 128
 - 2. Fill in 1 in corresponding digit, subtract 128 from the number => 106
 - 3. Repeat 1-2, until the number is 0
 - 4. Fill in empty digits with 0

•••	512	256	128	64	32	16	8	4	2	I
			1	1	1	0	1	0	1	0

Result is 11101010

Converting Binary to Decimal

Binary number system is base 2

- **▶** 0, 1
- Uses 2 numbers

10010001 = 145

Base 2 representation	27	26	25	24	23	22	21	20
Decimal representation	128	64	32	16	8	4	2	1
Base 2 representation	1	0	0	1	0	0	0	1

Binary to Decimal

- Technique
 - Multiply each bit by 2ⁿ, where n is the "weight" of the bit
 - The weight is the position of the bit, starting from 0 on the right
 - Add the results

 $101011_{2} \Rightarrow 1 \times 2^{0} = 1$ $1 \times 2^{1} = 2$ $0 \times 2^{2} = 0$ $1 \times 2^{3} = 8$ $0 \times 2^{4} = 0$ $1 \times 2^{5} = 32$ 43_{10}

Decimal Sayıların Binary Sayılara Çevrilmesi:

$$(172)_{10} = (128 + 32 + 8 + 4)_{10} = (2^7 + 2^5 + 2^3 + 2^2)_{10} = (1010 \ 1100)_2 = (AC)_{16}$$

Binary'den decimal'a çevirme örnekleri

• Örnek:

- (1010)2 = (?)10
- $(1010)2 = 1x2^3 + 0 \times 2^2 + 1 \times 2^1 \times 0x2^0$
- (1010)2 = 8 + 0 + 2 + 0
- (1010)2 = 10

• Örnek:

- (11001)2 = (?)10
- $(11001)2 = 1x2^4 + 1x2^3 + 0 \times 2^2 + 0x2^1 + 1x2^0$
- (11001)2 = 16 + 8 + 0 + 0 + 1
- (11001)2 = 25

Decimal sayı sisteminden binary sayı sistemine çevirme örnekleri

- (217)d=(?)b
- (217)d=(11011001)b
- Sağlaması:
- Maksimum ne var, 2^7=128
- 128+64+16+8+1=217
- İndislenir: 7 6 5 4 3 2 1 0 ise 2 üzeri olanlara 1 olmayanlar 0 yazılır.
- (11011001)b
- (54)d=(?)2
- 32+16+4+2
- (54)d=(110110)b



Hex Numbering System

Working with Large Numbers

- Humans can't work well with binary numbers; there are too many digits to deal with.
- Memory addresses and other data can be quite large. Therefore, we sometimes
 use the hexadecimal number system.
- The hexadecimal number system is also known as **base 16**. The values of the positions are calculated by taking 16 to some power.
- Why is the base 16 for hexadecimal numbers?
 - Because we use 16 symbols, the digits 0 and 1 and the letters A through F.

Hexadecimal System

The hexadecimal (hex) numbering system is used in programmable controllers because a word of data consists of 16 data bits, or two 8-bit bytes. The hexadecimal system is a base 16 system, with A to F used to represent decimal numbers 10 to 15. The hexadecimal numbering system allows the status of a large number of binary bits to be represented in a small space, such as on a computer screen.

The techniques used when converting hexadecimal to decimal and decimal to hexadecimal are the same as those used for binary and octal. To convert a hexadecimal number to its decimal equivalent, the hexadecimal digits in the columns are multiplied by the base 16 weight, depending on digit significance.

Groups of 4 bits

- Groups of bits can represent data or information
 - 1 bit 2 alternatives
 - 2 bits 4 alternatives
 - 3 bits 8 alternatives
 - 4 bits 16 alternatives
 - n bits 2ⁿ alternativies
 - 8bits -28 = 256 alternatives
 - a group of 8 bits is called a byte

4	Bits		
	0000		1000
•	0001		1001
•	0010		1010
•	0011		1011
•	0100		1100
•	0101		1101
•	0110		1110
•	0111	•	1111

Radix Number System

- Base -10 (Decimal numbering System) 0,1,2,, 9
- Base 2 (binary numbers), bit:0/1
 - **-** 01
- Base 8 (octal numbers)
 - -01234567
- Base 16 (hexadecimal numbers), 0 ve 1 lerin dizisinden oluşan ikil sayı sisteminde sağdan başlayarak 4'lü gruplar ayrılır.
 - 0123456789ABCDEF

Hex Sayı Sistemi Nedir?

- Binary ve desimal sistemden sonra mantık olarak aynı ancak fark olarak 16 lıkta bana sahip sayılar hexa desimal sayılardır.
- Heks sisteminde kullanabileceğimiz rakamlar benzer mantıkla yine 0,1,2,3,4,5,6,7,8,9,10,11,12,13,14,15 şeklindedir.
- Ancak hexa desimal sisteme göre yazılan sayılar 0,1,2,3,4,5,6,7,8,9,A,B,C,D,E,F, şeklindedir.
- Dijital Elektronikte binary sayıların heksa desimala çevrilip bellekte kodlanması sağlanır.
- Sayılar binary'den heksadesimale çevrilirken sağdan sola doğru dörder basamak olmak üzere gruplandırılır.
- Çünkü heksa decimal sayı sisteminin tabanı 16 dır ve binary sayı sisteminde 0-15 sayıları, 4 bit ile ifade edilebilmektedir.

Binary/Hexidecimal

Decimal	Binary	Hexidecimal
0	0000	0
1	0001	1
2	0010	2
3	0011	3
4	0100	4
5	0101	5
6	0110	6
7	0111	7
8	1000	8
9	1001	9
10	1010	A
11	1011	В
12	1100	С
13	1101	D
14	1110	Е
15	1111	F

Conversions:

1000 1110 (binary) <u>8</u> E (hex)

Notations for hex:

- 0x8E
- 8Eh
- 8E₁₆

Bilgisayarda, tüm işlevler 1/0 ikili sayı sisteminde. 1 ve 0 lardan oluşan dizi var.

- Giriş ve Çıkış
- Veri Transferi
- Saklama
- Manipülasyon (Aritmetk, Mantıksal; kontrol işlemleri, kesme, ...)

Veri: Sinyal (Ses, EM, Elektriksel, ..), Görüntü, Resim, Metin; portlar, klavvye, mouse

Numbers

- Short-hand for all these 1s and 0s
- HEX notation
- Hex is used as a notation for any sequence of bits (e.g. ASCII characters require just two hex digits)
- Each group of 4 bits represents a number in the range 0 15
- Thus: from right side to left side separate 4 digit.
- $(0000\ 0000\ 0000\ 1001)b = (0009)h$
- (1100 1011 1111 0111)b = (CBF7)h
- (0010 0110 1101 1011)b= (26DB)h

```
0000= 0 1000= 8

0001= 1 1001= 9

0010= 2 1010= A

0011= 3 1011= B

0100= 4 1100= C

0101= 5 1101= D

0110= 6 1110= E

0111= 7 1111= F
```

Hexadecimal numbers can easily be converted to binary numbers. Conversion is accomplished by writing the 4-bit binary equivalent of the hex digit for each position, as illustrated in Figure 6.7

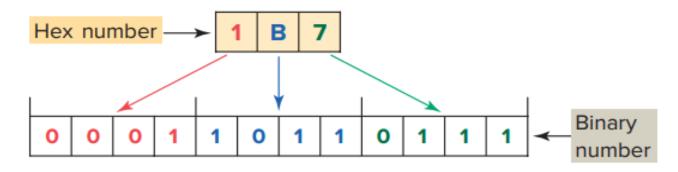


Figure 6.7 Converting a hexadecimal number to a binary number.

0000= 0 1000= 8 0001= 1 1001= 9 0010= 2 1010= A 0011= 3 1011= B 0100= 4 1100= C 0101= 5 1101= D 0110= 6 1110= E 0111= 7 1111= F

Table 6.5 Hexadecimal Numbering System

0. 0000 0 1. 0001 1 2. 0010 2 3. 0011 3 4. 0100 4 5. 0101 5 6. 0110 6 7. 0111 7 8. 1000 8 9. 1001 9 A. 1010 10 B. 1011 11 C. 1100 12 D. 1101 13 E. 1110 14 F. 1111 15	Hexadecimal	Binary	Decimal
2. 0010 2 3. 0011 3 4. 0100 4 5. 0101 5 6. 0110 6 7. 0111 7 8. 1000 8 9. 1001 9 A. 1010 10 B. 1011 11 C. 1100 12 D. 1101 13 E. 1110 14	0	0000	0
3. 0011 3 4. 0100 4 5. 0101 5 6. 0110 6 7. 0111 7 8. 1000 8 9. 1001 9 A. 1010 10 B. 1011 11 C. 1100 12 D. 1101 13 E. 1110 14	1	0001	1
4 0100 4 5 0101 5 6 0110 6 7 0111 7 8 1000 8 9 1001 9 A 1010 10 B 1011 11 C 1100 12 D 1101 13 E 1110 14	2		2
5.	3		3
6	4	0100	4
7.	5	0101	5
8. 1000 8 9. 1001 9 A. 1010 10 B. 1011 11 C. 1100 12 D. 1101 13 E. 1110 14	6	0110	6
9	7	0111	7
A	8	1000	8
B	9	1001	9
C	Α	1010	10
D	В	1011	11
E	C	1100	12
	D	1101	13
F	E		14
	F	1111	15

Figure 6.6 illustrates how the conversion would be done for the hex number 1B7

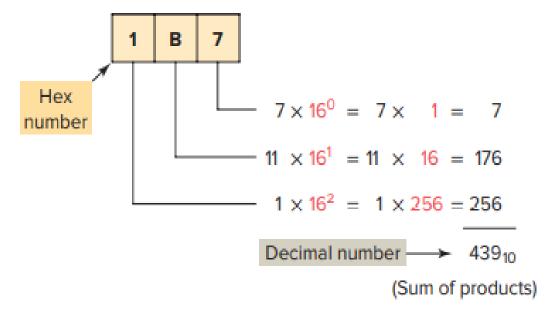


Figure 6.6 Converting a hexadecimal number to a decimal number.

Converting Binary Hexadecimal

Hex Binary

- Substitute hex digits, then drop leading zeros
- Example: 0x2D in binary
 - 0x2 is (0010)b, 0xD is (1101)b
 - Drop two leading zeros, answer is (0010 1101)b

Binary Hex

- Pad with leading zeros until multiple of 4, then substitute groups of 4
- Example: (101101)b
- Pad to (0010 1101)
- Substitute to get 0x2D

Base 10	Base 16	Base 2
0	0	0000
1	1	0001
2	2	0010
3	3	0011
4	4	0100
5	5	0101
6	6	0110
7	7	0111
8	8	1000
9	9	1001
10	Α	1010
11	В	1011
12	С	1100
13	D	1101
14	E	1110
15	F	1111

Binary Hex Practice

- Convert (0100 1101 1010 1101)b
- How many digits?
- Pad: (0100 1101 1010 1101)b
- Substitute: 0x4DAD
- Hexadecimal is shown different types: (...)h,
 (0x..)

Base 10	Base 16	Base 2
0	0	0000
1	1	0001
2	2	0010
3		0011
4	4	0100
5	5	0101
6	6	0110
7	7	0111
8	8	1000
9	9	1001
10	Α	1010
11	В	1011
12	С	1100
13	D	1101
14	E	1110
15	F	1111

Example of Equivalent Numbers

Hexadecimal: 50A7₁₆

Binary: 101 0000 1010 0111₂

İndis: 14 ... 210

Decimal: 20647₁₀

Notice how the number of digits gets smaller as the base increases.

Binary to Hexadecimal number system

Ex :- Convert the binary number
$$(1010101010)_2$$
 in to hexadecimal number.
 $(1010101010)_2 = 0010 \ 1010 \ 1010$
 $= (2AA)_{16}$

Converting Binary to Hexadecimal

- Mark groups of four (from right)
- Convert each group

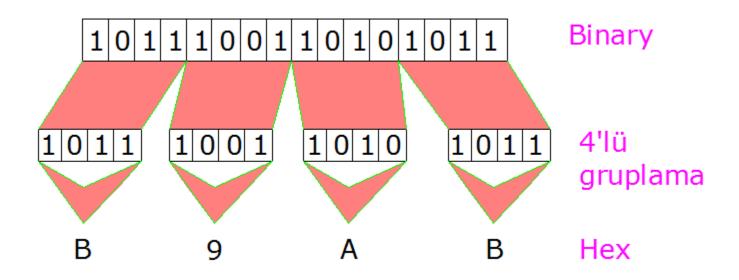
10101011

1010 1011 A B

10101011 is AB in base 16

And this?

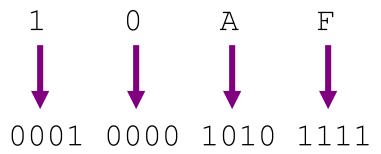
Binary Sayının Hexa decimal'e Çevrilmesi



Hexadecimal to Binary

Convert each hexadecimal digit to a 4-bit equivalent binary representation

$$10AF_{16} = ?_2$$



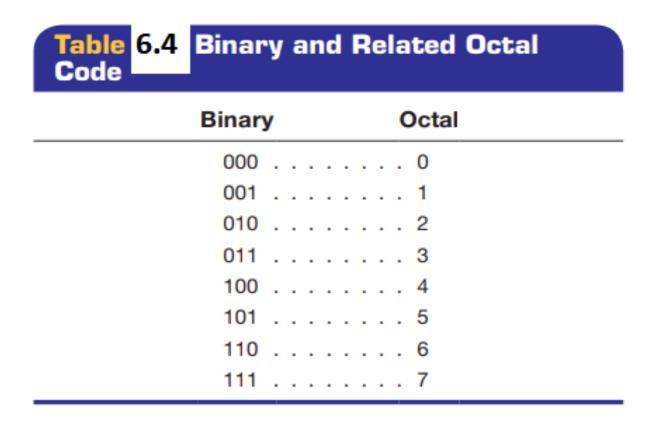
$$10AF_{16} = 0001000010101111_2$$

Octal System

Octal System

To express the number in the binary system requires many more digits than in the decimal system. Too many binary digits can become cumbersome to read or write. To solve this problem, other related numbering systems are used. The octal numbering system, a base 8 system, is used because 8 data bits make up a byte of information that can be addressed. Octal is a convenient means of handling large binary numbers

As shown in Table 6-4, one octal digit can be used to express three binary digits. As in all other numbering systems, each digit in an octal number has a weighted decimal value according to its position. Figure 6.6 illustrates how the octal number 462 is converted to its decimal equivalent: 306.



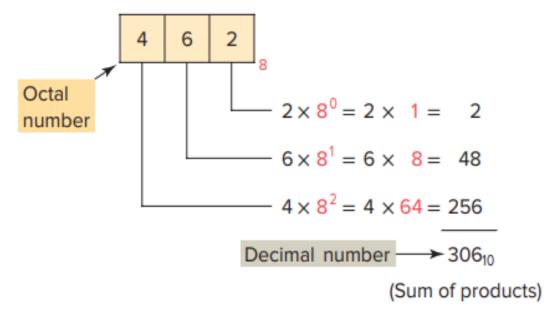


Figure 6.6 Converting an octal number to a decimal number.

Octal converts easily to binary equivalents. For example, the octal number 462 is converted to its binary equivalent by assembling the 3-bit groups, as illustrated in Figure 6.7.

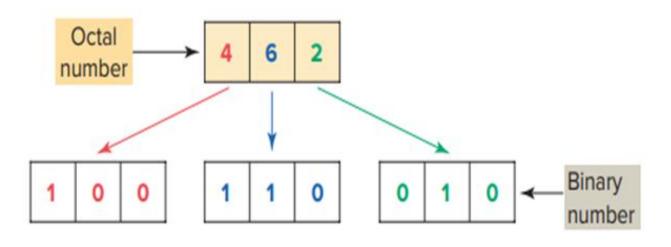
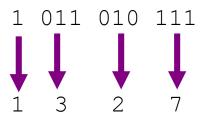


Figure 6. 7 Converting an octal number to a binary number.

Binary to Octal

- Technique
 - Group bits in threes, starting on right
 - Convert to octal digits

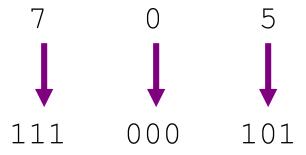
 $1011010111_2 = ?_8$



Octal to Binary

- Technique
 - Convert each octal digit to a 3-bit equivalent binary representation

$$705_8 = ?_2$$



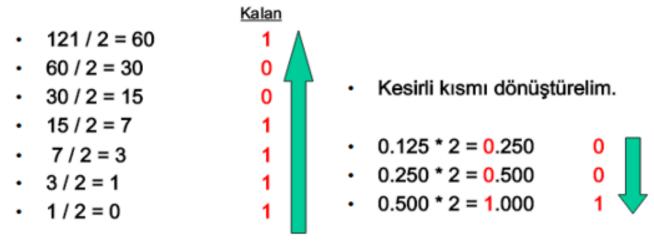
$$705_8 = 111000101_2$$

Fractions

Virgüllü ondalık sayıyı binarysayıya çevirme

- 10 tabanında verilen sayının tamsayı kısmı sürekli olarak istenen tabana bölünerek kalanlar sağdan sola doğru yazılır.
- 10 tabanında verilen sayının kesir kısmı için ise, bu kısım sürekli olarak istenen taban ile çarpılır ve çarpımın sonucu istenen basamağa erişene kadar (ya da 0 çıkana kadar) işlemin tamsayı kısmı alınır.
- Örnek: (121.125)10 sayısını 2 tabanına dönüştürünüz.

Sonuç = 1111001.001



Ondalık sayı sistemini ikil sayı sistemine dönüştürülürken 2'ye bölünerek en son böüm geröeklene devam edilir. Kalan var ise 1 yok ise 0 yapılır.

Here are some handy facts:

Power of 2	Base 2	Base 10
2 ⁻⁴ 2 ⁻³	.0001	.0625
2 ⁻³	.001	.125
2 ⁻²	.01	.25
2 ⁻¹	.1	.5
2°	1	1
2 ¹	10	2
2^2	100	4
2^{3}	1000	8
24	10000	16
25	100000	32
2 ⁶	1000000	64
27	10000000	128
28	100000000	256

N	Binary
0	0
1	1
2	10
3	11
4	100
5	101
6	110
7	111
8	1000
9	1001
10	1010
11	1011
12	1100
13	1101
14	1110
15	1111

Fractional Binary number to Decimal number

Ex :- Convert the binary number $(0.1101)_2$ into decimal number.

$$(0.1101)_2 = (1 \times \frac{1}{2}) + (1 \times \frac{1}{4}) + (0 \times \frac{1}{8}) + (1 \times \frac{1}{16})$$

$$= 1 \times 0.5 + 1 \times 0.25 + 0 \times 0.125 + 1 \times 0.0625$$

$$= 0.5 + 0.25 + 0 + 0.0625$$

$$= (0.8125)_{10}$$

Ex :- Convert the binary number $(1010.0101)_2$ into decimal number.

Sol:- Integer part
$$(1010)_2 = (1 \times 2^3) + (0 \times 2^2) + (1 \times 2^1) + (0 \times 2^0)$$

 $= (1 \times 8) + (0 \times 4) + (1 \times 2) + (0 \times 1)$
 $= (10)_{10}$
Fractional part $(0.0101)_2 = (0 \times 2^{-1}) + (1 \times 2^{-2}) + (0 \times 2^{-3}) + (1 \times 2^{-4})$
 $= (0 \times \frac{1}{2}) + (1 \times \frac{1}{4}) + (0 \times \frac{1}{8}) + (1 \times \frac{1}{16})$
 $= 0 \times 0.5 + 1 \times 0.25 + 0 \times 0.125 + 1 \times 0.0625$
 $= 0 + 0.25 + 0 + 0.0625$
 $= (0.3125)_{10}$

Fractional Decimal number to binary

The fractional decimal number is converted in to binary number by using successive fraction multiplications method.

- 1. The fractional decimal number is multiplied with 2 by successive fraction multiplications method.
- 2. If '1' or '0' occurs in units place in the product, transfer that '1' or '0' to the binary record.
- 3. The multiplication is continued with the remaining fraction.
- 4. The same procedure is followed in each multiplication.
- 5. The first transferred number (1 or 0) to binary record is taken as most significant bit (MSB).
- 6. The last transferred number (1 or 0) to binary record is taken as least significant bit (LSB).
- 7. If the multiplication does not end, it can be stopped at any of our desired level.

Ex: - Convert the fractional decimal number $(0.638)_{10}$ in to fractional binary number.

Sol:-

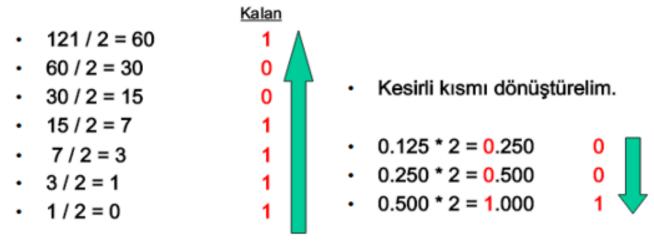
Successive multi	iplication:	s Bir	ary
$0.638 \times 2 = 1.276$		1	MSB
$0.276 \times 2 = 0.552$		0	
$0.552 \times 2 = 1.104$		1	
$0.104 \times 2 = 0.208$		0	
$0.208 \times 2 = 0.416$		0	
$0.416 \times 2 = 0.832$		0	
$0.832 \times 2 = 1.664$		1	
$0.664 \times 2 = 1.328$		1	
$0.328 \times 2 = 0.656$	*	0	
$0.656 \times 2 = 1.312$	-	1	LSB

So, $(0.638)_{10} = (0.1010001101)_2$

Virgüllü ondalık sayıyı binarysayıya çevirme

- 10 tabanında verilen sayının tamsayı kısmı sürekli olarak istenen tabana bölünerek kalanlar sağdan sola doğru yazılır.
- 10 tabanında verilen sayının kesir kısmı için ise, bu kısım sürekli olarak istenen taban ile çarpılır ve çarpımın sonucu istenen basamağa erişene kadar (ya da 0 çıkana kadar) işlemin tamsayı kısmı alınır.
- Örnek: (121.125)10 sayısını 2 tabanına dönüştürünüz.

Sonuç = 1111001.001



Ondalık sayı sistemini ikil sayı sistemine dönüştürülürken 2'ye bölünerek en son böüm geröeklene devam edilir. Kalan var ise 1 yok ise 0 yapılır.

Here are some handy facts:

Power of 2	Base 2	Base 10
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2 ⁻¹	.1	.5
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2^2	100	4
2^{3}	1000	8
24	10000	16
25	100000	32
2 ⁶	1000000	64
27	10000000	128
28	100000000	256

N	Binary
0	0
1	1
2	10
3	11
4	100
5	101
6	110
7	111
8	1000
9	1001
10	1010
11	1011
12	1100
13	1101
14	1110
15	1111

Fractions

- We can extend our unsigned representational system of binary to include a decimal point
 - After the decimal point, the i exponent, in 2ⁱ, becomes negative
 - So, we now have the ½ column, the ¼ column, etc
 - (1011.1001)b=
 - Indisleme: iki grupta yapılır. Noktadan sola ve sağa doğru... 3,2,1,0.,-1,-2,-3,-4
 - $-1*2^3+0*2^2+1*2^1+1*2^0+1*2^{-1}+0*2^{-2}+0*2^{-3}+1*2^{-4}=$
 - $-8+2+1+\frac{1}{2}+\frac{1}{16}=$
 - -119/16 = 11.5625
 - What is .4304? Use 8-bits with 4 fraction bits
 - .4304 has a .25, .125, .03125, .015625, and more fractions, but this exceeds the number of fraction bits so the number is 0000.0110
 - But 0000.0110 = .125 + 0.3125 = .375, we have a loss in precision!
 - In the fraction representation, our decimal point is typically fixed, so this is often known as *fixed point representation*
 - We will cover a floating point representation later

Fractions

Decimal to decimal (just for fun)
 Binary to decimal

3.14 =>
$$4 \times 10^{-2} = 0.04$$

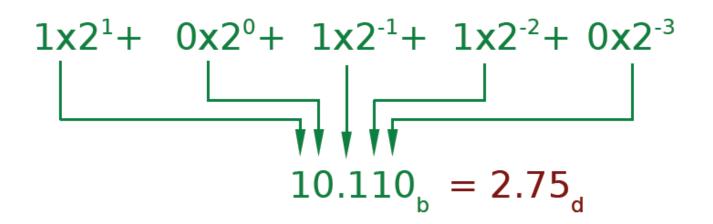
$$1 \times 10^{-1} = 0.1$$

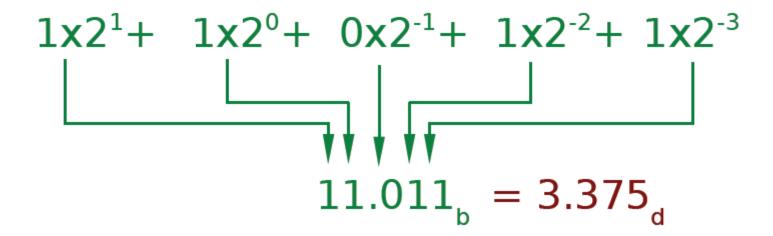
$$3 \times 10^{0} = 3$$

$$3.14$$

10.1011 => 1 x
$$2^{-4}$$
 = 0.0625
1 x 2^{-3} = 0.125
0 x 2^{-2} = 0.0
1 x 2^{-1} = 0.5
0 x 2^{0} = 0.0
1 x 2^{1} = 2.0
2.6875

Works for Fractional Numbers too...





Binary'den decimal'a çevirme örnekleri

- Örnek:
- (111,101)2 = (?)10
- (111,101)2 =
- $1x2^2 + 1x2^1 + 1 \times 2^0 + 1x2^{-1} + 0x2^{-2} + 1x2^{-3}$
- (111,101)2 =
- $1x4+1x2+1x1+1x\frac{1}{2}+0x\frac{1}{4}+1x\frac{1}{8}$
- (111,101)2 = 4+2+1+0,5+0+0,125
- (111,101)2 = (7,625)10

- Örnek:
- $(100111,01)_2$ =(?)₁₀
- $(100111,01)_2$ = $(39,25)_{10}$

Example: Digital Number Systems

• *Binary* numbers, Binary Digits = {0, 1}

Example: $(11010)_2 = (?)d=(?)h = (1A)h$

- Indexing: It is indexed from right to left.
- Indexing: 43210;
- When converting to the decimal number system, when adding expressions to the power of 2, multiply by 1 if the coefficient is 1 and by 0 if it is 0.
- Decimal value: $1 \times 2^4 + 1 \times 2^3 + 0 \times 2^2 + 1 \times 2^1 + 0 \times 2^0 = (26)d$

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Example: Float Point Digital Number Systems

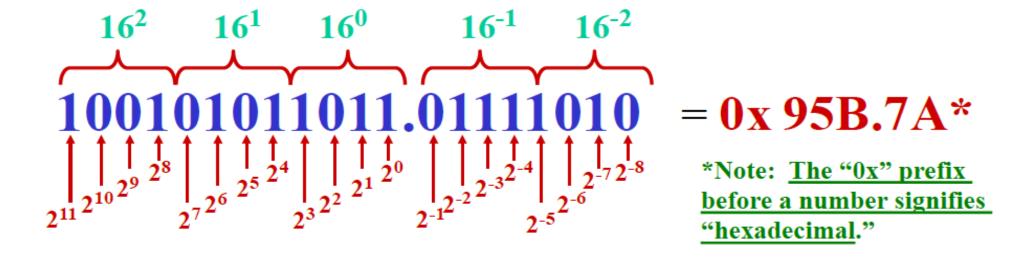
• *Binary* numbers

- Digits = $\{0, 1\}$
- $-(11010.11)_2 = ?$
- Indexing: It is indexed separately from the point to the left and right.
- Indexing: 43210.-1-2
- Decimal value: $1 \times 2^4 + 1 \times 2^3 + 0 \times 2^2 + 1 \times 2^1 + 0 \times 2^0 + 1 \times 2^{-1} + 1 \times 2^{-2}$ = $(26.75)_{10}$

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Binary-Hexadecimal

- Since $2^4 = 16$, each hex digit effectively represents the same numeric count as four binary digits.
- Another way to say this is that one column in a hex number is the same as four columns of a binary number.





Binary Aritmetic

Binary Arithmetic

Mathematical operations include addition, subtraction, multiplication, and division. Binary addition follows rules similar to decimal addition. When adding with binary numbers, there are only four conditions that can occur:

The first three conditions are easy because they are like adding decimals, but the last condition is slightly different. In decimal, 1 + 1 = 2. In binary, a 2 is written 10. Therefore, in binary, 1 + 1 = 0, with a carry of 1 to the next most significant place value. When adding larger binary numbers, the resulting 1s are carried into higher-order columns, as shown in the following examples.

Doing Binary Math.

0	0	1	1
<u>+0</u>	<u>+1</u>	<u>+0</u>	<u>+1</u>
0	1	1	10

Adding With A Carry

C _{i-1}	0	0	0	0	1	1	1	1
+a _i	0	0	1	1	0	0	1	1
<u>+b</u> i	+0	+1	+0	<u>+1</u>	+0	+1	+0	<u>+1</u>
T	0	1	1	10	1	10	10	11

Decimal

Equivalent binary

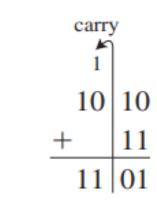
101

+ 10 111

10

13

26 38



In arithmetic functions, the initial numeric quantities that are to be combined by subtraction are the minuend and subtrahend. The result of the subtraction process is called the difference, represented as:

A (minuend)

(subtrahend)

(difference)

To subtract from larger binary numbers, subtract column by column, borrowing from the adjacent column when necessary. Remember that when borrowing from the adjacent column, there are now two digits, i.e., 0 borrow 1 gives 10.

EXAMPLE

Subtract 1001 from 1101.

 $\frac{1101}{-1001}$

Subtract O111 from 1011.

 $\frac{1011}{-0111}$ $\frac{-0100}{0100}$

EXAMPLE

Subtract 111 from 100.

 $\frac{111}{-100}$ $\frac{-100}{-011}$

Subtract 11011 from 10111.

 $\begin{array}{r}
 11011 \\
 -10111 \\
 -00100
 \end{array}$

Binary numbers can also be negative. The procedure for this calculation is identical to that of decimal numbers because the smaller value is subtracted from the larger value and a negative sign is placed in front of the result.

There are other methods available for doing subtraction:

1's complement

2's complement

The procedure for subtracting numbers using the 1's complement is as follows:

Step 1 Change the subtrahend to 1's complement.

Step 2 Add the two numbers.

Step 3 Remove the last carry and add it to the number (end-around carry)

When there is a carry at the end of the result is positive.

When there is no carry, we take the 1's complement of the result is and a minus

Sign has to be placed in front of it.

Binary 1010 -6 4 1010 -0110 1010 1010 1010 1001End-around carry 1001End-around carry

EXAMPLE

Subtract 11011 from 01101.

$$01101$$
 $+\cancel{0}00100$
The 1's complement

10001
There is no carry,
so we take the 1's
complement and add
the minus sign:
 -01110

For subtraction using the 2's complement, the 2's complement is added instead of subtracting the numbers. In the result, if the carry is a 1, then the result is positive; if the carry is a 0, then the result is negative and requires a minus sign.

EXAMPLE

Subtract 101 from 111.

EXAMPLE

Subtract 11011 from 01101.

 $01101 \\ + \varnothing 00101$ The 2's complement 10010 There is no carry, so the result is negative; therefore a 1 has to be subtracted and the 1's complement taken to give the result: subtract 1 10010 - 1 = 10001 1's complement -01110

REVIEW QUESTIONS

1. Convert each of the following binary number Convert each of the following decimal

1. Convert each of the following billary
to
decimal numbers:
a. 10
b. 100
c. 111
d. 1011
e. 1100
f. 10010
g. 10101
h. 11111
i. 11001101
i. 1110001

3. Convert each of the following octal numbers to decimal numbers:

a. 36

b. 104

c. 120

d. 216

e. 360

f. 1516

4. Convert each of the following octal numbers to binary numbers:

a. 74

b. 130

c. 250

d. 1510

e. 2551

f. 2634

5. Convert each of the following hexadecimal numbers to decimal numbers:

a. 5A

b. C7

c. 9B5

d. 1A6

6. Convert each of the following hexadecimal numbers to binary numbers:

a. 4C

b. E8

c. 6D2

d. 31B

- 7. Add the following binary numbers:
- a. 110 + 111
- b. 101 + 011
- c. 1100 + 1011
- 8. Subtract the following binary numbers:
- a. 1101 101
- b. 1001 110
- c. 10111 10010
- 9. Convert each piece of binary information to the
- appropriate hexadecimal code
- a. 0001 1111
- b. 0010 0101
- c. 0100 1110
- d. 0011 1001

- 10. Express the decimal number 18 in each of the following number codes:
- a. Binary
- b. Octal
- c. Hexadecimal

Bilgisayarda İşlemler

- Aritmetik: +, (-, *, /)
- Mantiksal: VE, VEYA, NOT, ...
- Karşılaştırma: <, >, ≥, ≤, ==, ≠, ...
- Mikroişlemci ALU (Aritmetik Logic Unit) sadece toplama işlemei vardır ve çarpma ve bölme işlemlerini ise öteleme ile yapar.
- ROL: Rotate operand1 left (Çarpma)

İkili Sayılarda Toplama

Binary(İkilik) sayı sistemindeki temel toplama kuralları;

Numerical examples for addition follow:

+ 6	00000110	- 6	11111010
+13	00001101	+13	00001101
+19	00010011	+ 7	00000111
+ 6	00000110	- 6	11111010
	00000110 11110011		11111010 11110011

Ondalık toplama işlemini düşünün: 3+1=4

İkili sayı sistemine dönüştürülür.

2 üssü toplamlardan ondalık sayı sistemi

eldeilir: 4=2^2

indisleme: 2 1 0

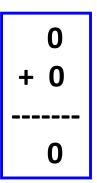
Dönüştürme: (100)

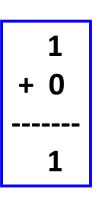
(3)d=(011)b

(1)d=(001)b

(011)b+(001)b=(100)b

Binary addition





Represent sum of binary numbers as a binary number

decimal addition

$$1+1 = 2$$

$$1+1+1=3$$

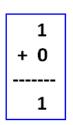
binary addition

$$1+1+1=10+1=11$$

Adding binary numbers

Binary addition

0 + 0 ------



Adding binary numbers

```
    Represent sum of binary numbers as a binary number
```

decimal addition

$$1+1=2$$

$$1+1+1=3$$

binary addition

Binary sayılarda toplama-çıkarma işlemleri

Aşağıda verilen toplama işlemlerini gerçekleştirin.

a-
$$(11)_2$$
 3 b- $(100)_2$ c- $(111)_2$ d- $(0110)_2$
 $\frac{+(11)_2}{(110)_2}$ $\frac{+(11)_2}{6}$ $\frac{+(11)_2}{(1010)_2}$ $\frac{+(1111)_2}{(10101)_2}$

Aşağıda verilen çıkarma işlemlerini gerçekleştirin.

a-
$$(11)_2$$
 b- $(100)_2$ c- $(101)_2$ d- $(1010)_2$
- $(10)_2$ - $(011)_2$ - $(011)_2$ - $(010)_2$ $(0111)_2$

c- (11101)₂

 $(1001)_2$

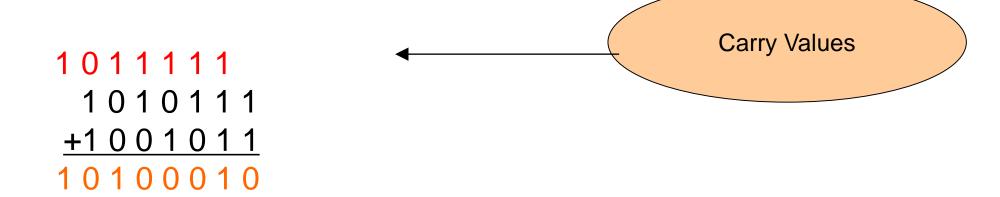
+ (1111)2

 $(101101)_2$

Arithmetic in Binary

Remember that there are only 2 digit symbols in binary, 0 and 1

1 + 1 is 0 with a carry



Subtracting Decimal Numbers

Anybody remember how to borrow in order to subtract two numbers?

Example: 271 - 196 = ?

Apply that same concept here:

```
12
202
1010111
- 111011
0011100
```

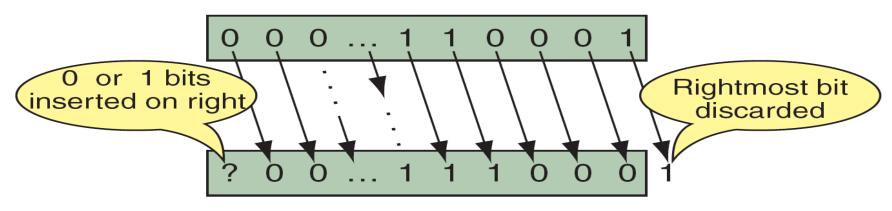
Adding Answers

110	1101	101110	1100101
+111	+1100	+110001	+1110001
1101	11001	1011111	11010110

Multipley and Division

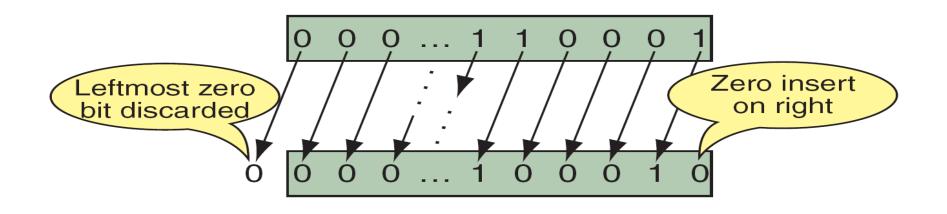
2 ^{shift} value	Divides by	Shift Operator
1	2	>> 1
2	4	>> 2
3	8	>> 3
4	16	>> 4
n	2 ⁿ	>> n

Divide by Shift



Multiply by Shift

2shift value	Multiplies by	Shift Operator
1	2	<< 1
2	4	<< 2
3	8	<< 3
4	16	<< 4
n	2 ⁿ	<< n



Soru

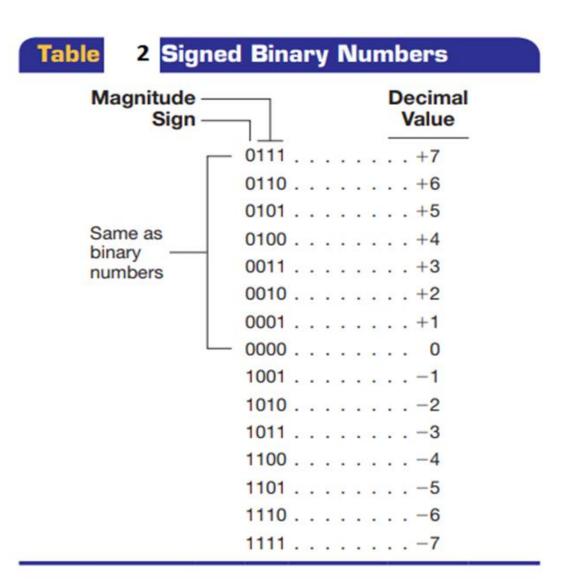
- (1011 0010)b=(?)d
- Bir bit sağdan sola öteleyin
- Bir bit soldan sağa öteleyin
- Yorumlayın

Negative Numbers

Twos Complement Representation Negatif Numbers

Negative Numbers

If a decimal number is positive, it has a plus sign; if a number is negative, it has a minus sign. In binary number systems, such as computers, it is not possible to use positive and negative symbols to represent the polarity of a number. One method of representing a binary number as either a positive or negative value is to use an extra digit, or sign bit, at the MSB side of the number. In the sign bit position, a 0 indicates that the number is positive, and a 1 indicates a negative number (Table 2)



Another method of expressing a negative number in a digital system is by using the complement of a binary number. To complement a binary number, change all the 1s to 0s and all the 0s to 1s. This is known as the 1's complement form of a binary number. For example, the 1's complement of 1001 is 0110. The most common way to express a negative binary number is to show it as a 2's complement number. The 2's complement is the binary number that results when 1 is added to the 1's complement. This system is shown in Table 6-3. A zero sign bit means a positive number, whereas a 1 sign bit means a negative number. Using the 2's complement makes it easier for the computer to perform mathematical operations. The correct sign bit is generated by forming the 2's complement.

Table 6.3 1's and 2's Complement Representation of Positive and Negative Numbers

Signed Decimal	1's Complement	2's Complement	2's Complement-16 bit
+7	0111	0111	0000 0000 0000 0111
+6	0110	0110	0000 0000 0000 0110
	0101		0000 0000 0000 0101
+4	0100 <mark>S</mark>	Same as 0100	0000 0000 0000 0100
	0011 n		0000 0000 0000 0011
+2	0010		0000 0000 0000 0010
+1	0001	0001	0000 0000 0000 0001
0		0000	0000 0000 0000 0000
-1	1110	1111	1111 1111 1111 1111
-2	1101	1110	1111 1111 1111 1110
-3	1100	1101	1111 1111 1111 1101
-4	1011	1100	1111 1111 1111 1100
-5	1010	1011	1111 1111 1111 1011
-6	1001	1010	1111 1111 1111 1010
-7	1000	1001	1111 1111 1111 1001

The computer knows that a number retrieved from memory is a negative number if the MSB is 1. Whenever a negative number is entered from a keyboard, the computer stores it as a 2's complement. What follows is the original number in true binary followed by its 1's complement, its 2's complement, and finally, its decimal equivalent

Unsigned Binary Integers

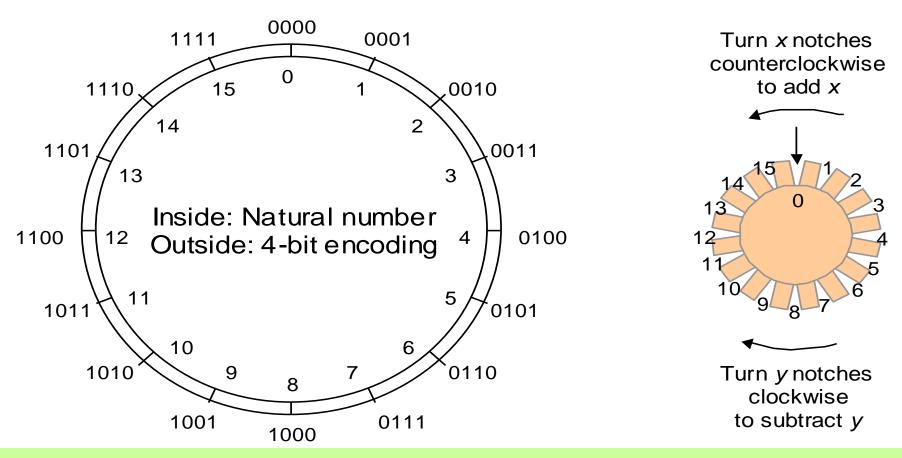


Figure Schematic representation of 4-bit code for integers in [0, 15].

Two's-Complement Representation

With k bits, numbers in the range $[-2^{k-1}, 2^{k-1} - 1]$ represented. Negation is performed by inverting all bits and adding 1.

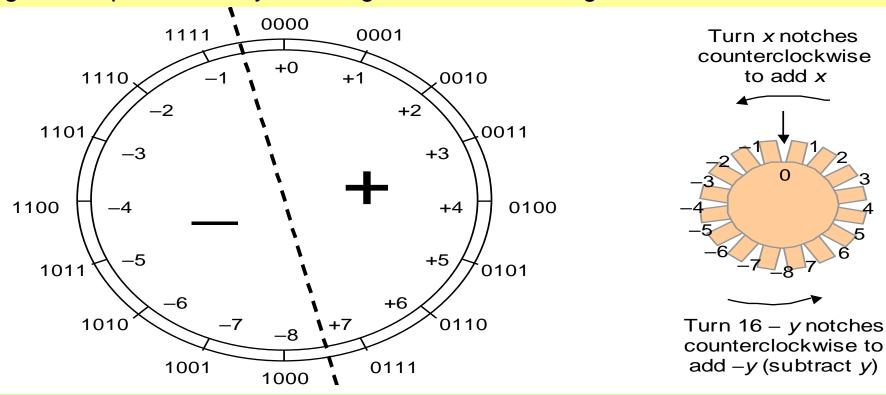


Figure Schematic representation of 4-bit 2's-complement code for integers in [-8, +7].

Fixed-Point 2's-Complement Numbers

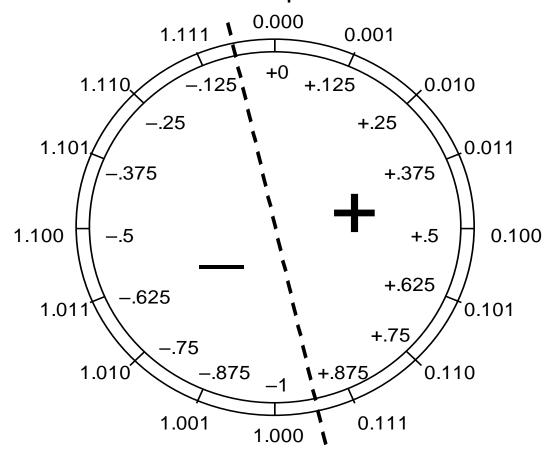
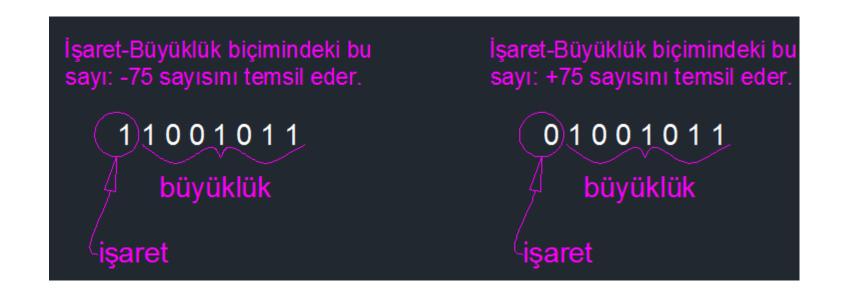
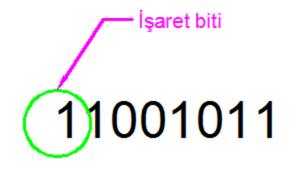


Figure Schematic representation of 4-bit 2's-complement encoding for (1 + 3)-bit fixed-point numbers in the range [-1, +7/8].

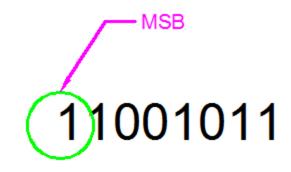
İşaretli binary sayılar

- İkili sayı sistemlerinde 1 byt eile (8 bit) 0-255 arası pozitif sayıları ifade edebiliriz, fakat
- negatif sayıları ifade etmek için kullanıldığında en soldaki bit işaret bitidir.
- Eğer işaret biti 1 ise sayı negatif, 0 ise sayı pozitiftir.





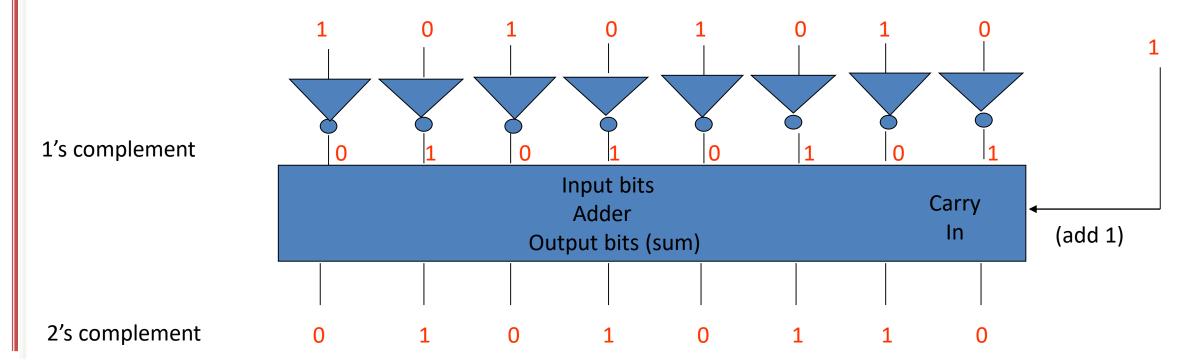
(signed char olarak tanımlamalarda)



(unsigned char olarak tanımlamalarda)

Complements of Binary Numbers

- 2's complement
- Find 1's complement and then add 1



İşaretli (signed) binary sayıların bir gösterim şekli de işaret-büyüklük biçiminde gösterimdir.

ÖRNEK: +19 ve -19 desimal sayılarını işaret-büyüklük formunda 1 byte binary sayı ile ifade ediniz.

- Çözüm:
- (19)10=16+3=16+2+1=2^4+2^1+2^0;
- İndisleme:4,3,2,1,0
- (10011)2
- (+19)d= (00010011)b
- (-19)d=(?)b Not: 8, 16, 32, 64 bit düzeninde işlem yapılır.
- (+19)d=(00010011)b -> ikil sayı sisteminde tersi alınır; 1->0, 0 ->1 konur. Sonra +1 eklenir.
- (-19)d=(11101100)b +1= (1110 1101)b

Negatif Sayıların ikil sayı sistemine çevrilmesi

- Önce negatif işareti olmadan ondalık sayıyı ikili sayı sistemine çevrilir.
- En sağdan başlayarak dörterli gruplara ayrılır.
- En soldaki bit 1 ise 0'lar ilave ederek dörtlü gruba tamamlanır ya da sıfırlardan oluşan yeni bir dörtlü grup ilave edilir. (8, 16, 32, 64, ...)
- Elde ettiğiniz ikili sayı sisteminde 1 yerine 0; 0 yerine 1 yazılır.
- Son olarak yeni ikili sayı sistemi +1 ile toplanır.

```
+18 = 0001 \ 0010 \ (twos \ complement) bitwise complement = 1110 1101 \frac{+}{1110 \ 1110} = -18 -18 = 1110 \ 1110 \ (twos \ complement) bitwise complement = 0001 0001 + 1 0001 0010 = +18
```

Negatif sayılar

- Byte: 8 bit data tanımlar; 8 bitlik bellek gözünü işaret eder.
- Örnek db -4
 (4)d= (0000 0100)b
 (-4)d= Binary (4) Tersi +1:
 (-4)d = 1111 1011 +1 = 1111 1100=(FC)h
- Örnek dW -4

 (4)d= (0000 0000 0000 0100)b
 (-4)d=Word(4) Tersi +1
 (-4)d=(1111 1111 1111 1011)b +1= (1111 1111 1111 1100)b=(FFFC)h

Overflow

- Taşma, toplamdaki bit sayısı, toplanan ve artırılan bitlerin sayısını aştığında meydana gelir.
- Taşma, yanlış işaret ile gösterilir. Yalnızca her iki sayı da pozitif olduğunda veya her iki sayı da negatif olduğunda oluşur



Coding

Kodlama

- 0 ile 9arasındaki ikil sayı sistemi kullanılır.
- Genel olarak kodlama, görülebilen, okunabilen, yazı, sayı ve işaretlerin değiştirilmesi olarak tanımlanır.
- Binary Coded Decimal Kodlaması(BCD) sisteminde her desimalsayı karakteri için, dört bit kullanılır.

Decimal	BCD				
25			0010	0101	
32			0011	0010	
679		0110	0111	1001	
2571	0010	0101	0111	0001	

<u>Decimal</u> Sayıları	BCD Kodu
О	0000
1	0001
2	0010
3	0011
4	0100
5	0101
6	0110
7	0111
8	1000
9	1001

Characters and Other Codes

- To represent information as strings of alpha-numeric characters.
- Binary Coded Decimal (BCD)
 - Used to represent the decimal digits 0 9.
 - 4 bits are used.
 - Each bit position has a weight associated with it (weighted code).
 - Weights are: 8, 4, 2, and 1 from MSB to LSB (called 8-4-2-1 code).
 - BCD Codes:

```
0: 0000 1: 0001 2: 0010 3: 0011 4: 0100 5: 0101 6: 0110 7: 0111 8: 1000 9: 1001
```

- Used to encode numbers for output to numerical displays
- Used in processors that perform decimal arithmetic.
- **Example**: $(9750)_{10} = (1001011101010000)_{BCD}$

BCD kodlama örnekleri

Örnek: (10100110)2sayısını BCD koduna çeviriniz.

- Binary sayıyı ilk olarak desimale çevirelim;
- 2+4+32+128=166
- (10100110)2= (166)10
- BCD koduna çevirirsek
- (000101100110)*BCD*

Örnek: (1010110101)2sayısını BCD koduna çeviriniz.

- Binarysayıyı ilk olarak desimaleçevirelim;
- 1+4+16+32+128+512=693
- (1010110101)2= (693)10
- BCD koduna çevirirsek
- (011010010011)*BCD* bulunur.

0 -12 Decimal sayıları için Gray kodlaması

- Birinci bit aynen aşağıya indirilir,
- ikinci bit aşağıya indirilen bit ile toplanır ve sonuç hemen aşağıya indirilen birinci bitin sağına yazılır.
- Üçüncü bit, aşağıya yazılan ikinci bit ile toplanır ve ikinci bit 'in yanına yazılır.
- son bite kadar işlem böyle devam ettirilir.

Örnek:(011010111101)2sayısını graykoduna çeviriniz.

- İlk rakam aynen alınır,
- Diğer basamaklarda sayı değişiyorsa 1, sayı değişmiyorsa 0 alınarak sonuca ulaşılır.
- (011010111101)2
- (010111100011)*gray*

Örnek:(1110001101101)2sayısını graykoduna çeviriniz.

- İlk rakam aynen alınır,
- Diğer basamaklarda sayı değişiyorsa 1, sayı değişmiyorsa 0 alınarak sonuca ulaşılır.
- (1110001101101)2
- (1001001011011)*gray*

Örnek: 297 decimalsayısını graykodu ile kodlayınız?

(297)10= (100101001)2

(100101001)2=(110111101)gray

Decimal	Binary	Gray
0	0000	0000
1	0001	0001
2	0010	0011
3	0011	0010
4	0100	0110
5	0101	0111
6	0110	0101
7	0111	0100
8	1000	1100
9	1001	1101
10	1010	1111
11	1011	1110
12	1100	1010

Gray Kodu

- Gray kodunun, sütun taraması esasına göre çalışan cihazlarda oldukça geniş bir kullanım alanı vardır.
- Geçişler sırasında hatayı minimuma indirmek için geliştirilmiş bir koddur. İsmini mucidi Frank GRAY'den alır.
- Özelliği, Ardarda iki sayı arasında sadece tek bit değişikliğidir.
- Normal Binary kodunda ardışık sayılarda çoğu kez birden fazla bit değişikliği söz konusudur. Devrelerde 0-1 durumları arasındaki değişim sırasında okuyucu farklı değerler okuyabilir.
- Gray kodunda sadece tek bit değiştiğinden, ve binary sayı olduğundan, gray kodunda bu hata ortadan kaldırılmıştır.

Graykodu ile kodlanmış sayıyı tekrar elde etme örnekleri

Örnek: (01011101) gray graykodlu sayıyı binary'e çevirelim.

- (01011101)*gray*
- (01101001)2
- İlk sayı aynen aşağı alınır,
- Sağındaki diğer sayılar
- yukarıdaki sayı 1 olduğunda rakamın değiştiğine,
- 0 olduğunda değişmediğine alamet olarak değerlendirilir.

Örnek: (10101100111)*gray*

- graykodlu sayıyı binary'eçevirelim.
- (10101100111)*gray*
- (11001000101)2

Characters and Other Codes

Gray Code

- Cyclic code: A circular shifting of a code word produces another code word.
- Gray code: A cyclic code with the property that two consecutive code words differ in only 1 bit (the distance between the two code words is 1).
- Gray code for decimal numbers 0 15: See Table 1.12

ASCII Character Code

ASCII Character Code

- Digital computers handle not only the numbers, but also other characters or symbols, such as the letters of the alphabet.
- An alphanumeric character set is a set of elements that includes the 10 decimal digits, the 26 letters of the alphabet, and a number of special characters. Such a set contains between 36 and 64 elements if only capital letters are included, or between 64 and 128 elements if both uppercase and lowercase letters are included.
- The American Standard Code for Information Interchange (ASCII) uses seven bits to code 128 characters, as shown in Table 1.
- The 7 bits of the code are designated by b1 through b7, with b7 the most significant bit.
- The letter A, for example, is represented in ASCII as (1000001)b (column 100, row 0001).
- The ASCII code also contains 94 graphic characters that can be printed and 34 nonprinting characters used for various control functions.
- The graphic characters consist of the 26 uppercase letters (A through Z), the 26 lowercase letters (a through z), the 10 numerals (0 through 9), and 32 special printable characters, such as %, *, and \$.

There needs a standard way

- ASCII code: American Standard Code for Information Interchange
 - ASCII codes represent <u>text</u> in <u>computers</u>, <u>communications</u> equipment, and other devices that use text.
 - ASCII kodları, bilgisayarlardaki, klavyedeki tüm tuşların 8 bitlik değerini temsil eder. Böylece klavyedeki tuşlar ile bellek arasındaki iletişim sayısal olarak yapılmış olur.
 - 128 characters:
 - 33 are non-printing <u>control characters</u> (now mostly obsolete)^[7] that affect how text and space is processed
 - 94 are printable characters
 - <u>space</u> is considered an invisible graphic

ASCII Coding

- Bilgisayarda 0 ve 1'lerle karakterleri ifade etmek için ikili kodlama sistemleri kullanılır.
- ASCII, karakterleri göstermek için sekiz bit (bir bayt) kullanır. Yeni geliştirilen Unicode ise karakterleri göstermek için onaltı bit kullanır:
- ASCII (American Standard Code for Information Interchange bilgi değişimi için Amerikan standart kodlaması)
- EBCDIC (Extended Binary Coded Decimal Interchange Code genişletilmiş ikili kodlamalı onluk sistem değiştirme kodlaması): IBM şirketi tarafından ana bilgisayarlarda kullanılmak için geliştirilmiştir.
- Unicode: Çince ve Japonca gibi dilleri desteklemek için tasarlanmış onaltı bit kullanan kodlamadır. Bu diller sekiz bit kullanan ASCII ve EBCDIC kodlamaları ile gösterilemeyecek kadar çok sayıda karakter kullanırlar. Unicode kodlaması, IBM, Apple ve Microsoft şirketlerinin desteklediği Unicode şirketi tarafından geliştirilmiştir.

<u>Kodlama</u>	<u>Kullanımı</u>				
ASCII	Kişisel bilgisayarlar				
EBCDIC	Anabilgisayarlar				
Unicode	Uluslararası diller				

- Klavyede bir tuşa bastığınız zaman, tuşa karşılık gelen karakter, bilgisayarın anlayabileceği bir dizi bite çevirilir. Örneğin, klavyede A harfine basmak bilgisayar bunu (41)h=(01000001)b ASCII koduna çevirir.
- Dökümanlar değişik bilgisayarlar veya uygulama programları tarafından paylaşıldığı zaman, aynı kodlama sistemi kullanılmalıdır.

ASCII Character Set

American Standard Code for Information Interchange (ASCII)

	$b_7b_6b_5$							
$b_4b_3b_2b_1$	000	001	010	011	100	101	110	111
0000	NUL	DLE	SP	0	@	P	`	p
0001	SOH	DC1	!	1	A	Q	a	q
0010	STX	DC2	66	2	В	R	b	r
0011	ETX	DC3	#	3	C	S	c	S
0100	EOT	DC4	\$	4	D	T	d	t
0101	ENQ	NAK	%	5	E	U	e	u
0110	ACK	SYN	&	6	F	V	\mathbf{f}	\mathbf{v}
0111	BEL	ETB	4	7	G	W	g	W
1000	BS	CAN	(8	\mathbf{H}	X	h	X
1001	HT	EM)	9	I	Y	i	y
1010	LF	SUB	*	:	J	Z	j	Z
1011	VT	ESC	+	;	K	[k	{
1100	FF	FS	,	<	L	\	1	Ĭ
1101	CR	GS	_	=	M]	m	}
1110	SO	RS		>	N	\wedge	n	~
1111	SI	US	/	?	O	_	O	DEL

ASCII Character Codes (2)

Hex	Char	Hex	Char	Hex	Char	Hex	Char	Hex	Char	Hex	Char
20	(Space)	30	0	40	@	50	Р	60		70	р
21	!	31	1	41	Α	51	Q	61	а	71	q
22	II .	32	2	42	В	52	R	62	b	72	r
23	#	33	3	43	С	53	S	63	С	73	s
24	\$	34	4	44	D	54	Т	64	d	74	t
25	%	35	5	45	E	55	U	65	е	75	u
26	&	36	6	46	F	56	V	66	f	76	v
27	,	37	7	47	G	57	W	67	g	77	w
28	(38	8	48	Н	58	X	68	h	78	X
29)	39	9	49	- 1	59	Υ	69	i	79	у
2A	*	ЗА	:	4A	J	5A	Z	6A	j	7A	z
2B	+	3B	;	4B	K	5B]	6B	k	7B	{
2C	,	3C	<	4C	L	5C	\	6C	- 1	7C	
2D	-	3D	=	4D	М	5D]	6D	m	7D	}
2E		3E	>	4E	Ν	5E	^	6E	n	7E	~
2F	/	3F	?	4F	0	5F	_	6F	0	7F	DEL

The ASCII Character set: characters 32 – 127.

Dec	Hex	Char	Dec	Hex	Char	Dec	Hex	Char	Dec	Hex	Char
0	00	Null	32	20	Space	64	40	0	96	60	`
1	01	Start of heading	33	21	!	65	41	A	97	61	a
2	02	Start of text	34	22	**	66	42	В	98	62	b
3	03	End of text	35	23	#	67	43	С	99	63	c
4	04	End of transmit	36	24	Ş	68	44	D	100	64	d
5	05	Enquiry	37	25	*	69	45	E	101	65	e
6	06	Acknowledge	38	26	ھ	70	46	F	102	66	£
7	07	Audible bell	39	27	1	71	47	G	103	67	g
8	08	Backspace	40	28	(72	48	Н	104	68	h
9	09	Horizontal tab	41	29)	73	49	I	105	69	i
10	OA	Line feed	42	2A	*	74	4A	J	106	6A	j
11	OB	Vertical tab	43	2B	+	75	4B	K	107	6B	k
12	oc	Form feed	44	2C	,	76	4C	L	108	6C	1
13	OD	Carriage return	45	2 D	_	77	4 D	M	109	6D	m
14	OE	Shift out	46	2 E		78	4E	N	110	6E	n
15	OF	Shift in	47	2 F	/	79	4F	0	111	6F	0
16	10	Data link escape	48	30	0	80	50	P	112	70	p
17	11	Device control 1	49	31	1	81	51	Q	113	71	a
18	12	Device control 2	50	32	2	82	52	R	114	72	r
19	13	Device control 3	51	33	3	83	53	S	115	73	s
20	14	Device control 4	52	34	4	84	54	Т	116	74	t
21	15	Neg. acknowledge	53	35	5	85	55	U	117	75	u
22	16	Synchronous idle	54	36	6	86	56	v	118	76	v
23	17	End trans, block	55	37	7	87	57	ឃ	119	77	w
24	18	Cancel	56	38	8	88	58	x	120	78	×
25	19	End of medium	57	39	9	89	59	Y	121	79	У
26	1A	Substitution	58	ЗА	:	90	5A	Z	122	7A	z
27	1B	Escape	59	3B	;	91	5B	С	123	7B	{
28	1C	File separator	60	3 C	<	92	5C	١	124	7C	ı
29	1D	Group separator	61	ЗD	=	93	5D]	125	7D	}
30	1E	Record separator	62	ЗЕ	>	94	5E	^	126	7E	~
31	1F	Unit separator	63	3 F	?	95	5F	_	127	7F	

Bits as Codes

- Asciikodu bizim bilgisayarda görsel olarak girdiğimiz karakter,harfve rakamların bilgisayar dilindeki temsil edilme şeklidir diyebiliriz.
- Yani bilgisayarımızın o karakteri, harfi veya rakamı belleğinde saklama biçimidir,
- Açılımı ASCII (AmericanStandard CodeforInformation Interchange)olan
- Bu kodlama sistemi ilk olarak telgraf kodlarında kullanılmıştır
- Klavyedeki her tuşun 8 bitlik bir karşılığı vardır.
- İkili Kodlar her harf, rakam ve özel karakteri temsil eder.
- ASCII: Her karakter benzersiz bir 8 bitlik koddur
- AsCII: 26 harf, 10 hane, özel karakterler için 256 benzersiz kod
- Unicode: 100.000'den fazla benzersiz karakteri destekler.
- Klavyeden girilen her karakter bilgisayara ASCII kodu ile giriş yapar.

ASCII	SYMBOL	ASC
00110000	0	010
00110001	1	010
00110010	2	010
00110011	3	010
00110100	4	010
00110101	5	010
00110110	6	010
00110111	7	010
00111000	8	010
00111001	9	010
01000001	A	010
01000010	В	010
01000011	C	010
01000100	D	001
01000101	E	001
01000110	F	001
01000111	G	001
01001000	Н	001
01001001		001
01001010	J J	001
01001011	K	001
01001100	L	001
01001101	M	001

ASCII	SYMBOL
01001110	N
01001111	0
01010000	P
01010001	Q
01010010	R
01010011	S
01010100	T
01010101	U
01010110	V
01010111	W
01011000	X
01011001	Y
01011010	Z
00100001	
00100010	
00100011	#
00100100	\$
00100101	%
00100110	&
00101000	
00101001)
00101010	*
00101011	+



Hamming Codes

Hamming Codes (1)

- Multiple check bits are employed.
- Each check bit is defined over (or covers) a subset of the information bits.
- Subsets overlap so that each information bit is in at least two subsets.
- d_{min} is equal to the weight of the minimum-weight nonzero code word.

Hamming Code 1

- $-d_{min}$ = 3, single error correction code.
- Let the set of all code words: C an error word with single error: c_e the correct code word for the error word: c

then, $d(c_e, c) = 1$ and $d(c_e, w) > 1$ for all other $w \in C$

 So, a single error can be detected and corrected by finding out the code word which differs in 1 bit position from the error word.

Hamming Codes (2)

A code word consists of 4 information bits and 3 check bits:

$$c = (i_3 i_2 i_1 i_0 c_2 c_1 c_0)$$

– Each check bit covers:

$$C_2$$
: i_3 , i_2 , i_1 C_1 : i_3 , i_2 , i_0 C_0 : i_3 , i_1 , i_0

This relationship is specified by the generating matrix, G:

$$G = \begin{bmatrix} 1000111 \\ 0100110 \\ 0010101 \\ 0001011 \end{bmatrix} = \begin{bmatrix} 1000p_{11}p_{12}p_{13} \\ 0100p_{21}p_{22}p_{23} \\ 0010p_{31}p_{32}p_{33} \\ 0001p_{41}p_{42}p_{43} \end{bmatrix}$$

Encoding of an information word i to produce a code word, c:

$$c = iG$$

Hamming Codes (3)

Decoding can be done using the parity-check matrix, H:

$$H = \begin{bmatrix} p_{11}p_{21}p_{31}p_{41}100 \\ p_{12}p_{22}p_{32}p_{42}010 \\ p_{13}p_{23}p_{33}p_{43}001 \end{bmatrix} = \begin{bmatrix} 1110100 \\ 1101010 \\ 1011001 \end{bmatrix}$$

- H matrix is can be derived from G matrix.
- An n-tuple c is a code word generated by G if and only if

$$Hc^T = 0$$

Let d be a data word corresponding to a code word c, which has been corrupted by an error pattern e.
 Then

$$d = c + e$$

- Decoding:
 - Compute the syndrome, *s*, of *d* using *H* matrix.
 - *s* tells the position of the erroneous bit.

Hamming Codes (4)

– Computation of the syndrome:

$$s = Hd^{T}$$

$$= H(c + e)^{T}$$

$$= Hc^{T} + He^{T}$$

$$= 0 + He^{T}$$

$$= He^{T}$$

• Note: All computations are performed using modulo-2 arithmetic.

Hamming Codes (5)

Hamming Code 2)

- $-d_{min}$ = 4, single error correction and double-error detection.
- The generator and parity-check matrices are:

$$G = \begin{bmatrix} 10000111 \\ 01001110 \\ 00101101 \\ 00011011 \end{bmatrix}$$

$$H = \begin{bmatrix} 01111000 \\ 11100100 \\ 11010010 \\ 10110001 \end{bmatrix}$$

Odd-weight-column code:

- H matrix has an odd number of ones in each column.
- Example: Hamming Code 2.
- Has many properties; single-error correction, double-error detection, multiple-error detection, low cost encoding and decoding, etc.

Hamming Codes (6)

- Hamming codes are most easily designed by specifying the H matrix.
- For any positive integer $m \ge 3$, there exists an (n, k) SEC Hamming code with the following properties:
 - Code length: $n = 2^m 1$
 - Number of information bits: $k = 2^m m 1$
 - Number of check bits: n k = m
 - Minimum distance: $d_{min} = 3$
- The H matrix is an $n \times m$ matrix with all nonzero m-tuples as its column.
- A possible H matrix for a (15, 11) Hamming code, when m = 4:

Hamming Codes (7)

- **Example**: A Hamming code for encoding five (k = 5) information bits.
 - Four check bits are required (m = 4). So, n = 9.
 - A (9, 5) code can be obtained by deleting six columns from the (15,11) code shown above.
 - The H and G matrices are:

$$H = \begin{bmatrix} 1111101000 \\ 111010100 \\ 110110010 \\ 101110001 \end{bmatrix} G =$$

$$G = \begin{bmatrix} 100001111 \\ 010001110 \\ 001001101 \\ 00010111 \\ 000010111 \end{bmatrix}$$

ROR: Rotate operand1 right (Bölme)

- ROR Operand1, Operand2
- Algorithm: Tüm bitleri sağa kaydırılır, giden bit CF'ye ayarlanır ve aynı bit en soldaki konuma eklenir.
- Not: Operand1'i sağa döndürülür. Döndürme sayısı Operand2 tarafından belirlenir.

Operand1, Operand2:

- memory, immediate
- REG, immediate
- memory, CL
- REG, CL

• Example:

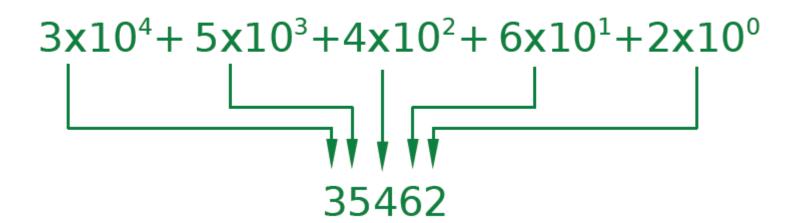
```
MOV AL, 1Ch; AL = 00011100b
ROR AL, 1; AL = 00001110b, CF=0.
RET
```

Decimal Number System

İndis sağdan başlar; 0,1,2,3,4, ...

Neden indis O'dan başlar? Birler basamağı 10^0=1

Herbir katsayı ile 10'indis .arpılıp toplandığında ondalık sayının kendisi elde edilir.





Karekod(barkod)

Karekod(barkod)

- Karekod, kare veya dikdörtgen biçimlerde basılabilen 2 boyutlu barkodun ismidir. Kare veya dikdörtgen şeklinde olan bu yapının genel adı ise Data Matrixtir.
- Karekodkelimesi ilk olarak, Beşeri Tıbbi Ürünler Barkod Uygulama Kılavuzunda kullanılmıştır.
- Ülkemizdeki ilk uygulama alanı, ilaç sektörüdür.
- Karekodbarkodların başlıcaları; QR Kod, Data MatrixKod, AztekKod







- An error: An incorrect value in one or more bits.
- Single error: An incorrect value in only one bit.
- *Multiple error*: One or more bits are incorrect.
- Errors are introduced by hardware failures, external interference (noise), or other unwanted events.
- *Error detection/correction code*: Information is encoded in such a way that a particular class of errors can be detected and/or corrected.
- Let *I* and *J* be *n*-bit binary information words
 - w(I): the number of 1's in I (weight)
 - -d(I, J): the number of bit positions in which I and J differ (distance)
- **Example**: I = (01101100) and J = (11000100)
 - w(I) = 4 and w(J) = 3
 - -d(I,J)=3.

General Properties

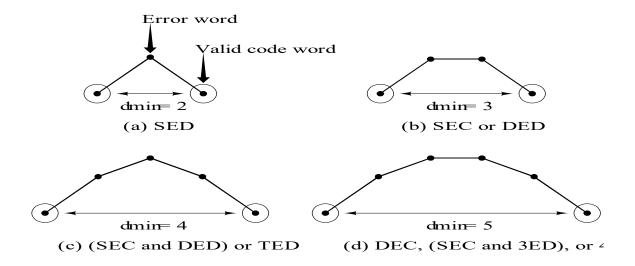
- Minimum distance, d_{min} , of a code C: for any two code words I and J in C, $d(I, J) \ge d_{min}$
- A code provides t error correction plus detection of s additional errors if and only if the following inequality is satisfied.

$$2t + s + 1 \le d_{min} \tag{1.25}$$

- Example:

- Single-error detection (SED): s = 1, t = 0, $d_{min} = 2$.
- Single-error correction (SEC): s = 0, t = 1, $d_{min} = 3$.
- Single-error correction and double-error detection (SEC and DED): s = t = 1, $d_{min} = 4$.

• Relationship between the minimum distance between code words and the ability to detect and correct errors:



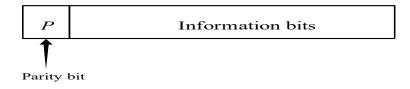
• Simple Parity Code

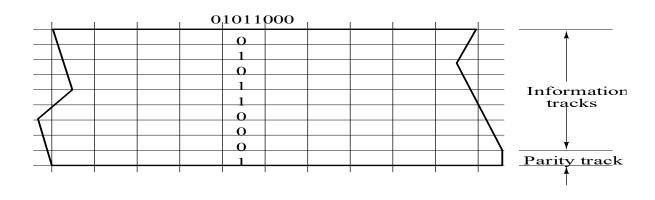
Concatenate (|) a parity bit, P, to each code word of C.



- Even-parity code: w(P|C) is even.

– Parity coding on magnetic tape:





— Example: Odd-parity code for ASCII code characters:

Character	ASCII Code	Odd-parity Code
О	0110000	10110000
X	1011000	01011000
=	0111100	1111100
BEL	0000111	00000111

- Error detection: Check whether a code word has the correct parity.
- Single-error detection code ($d_{min} = 2$).

• Two-out-of-Five Code

- Each code word has exactly two 1's and three 0's.
- Detects single errors and multiple errors in adjacent bits.

Check Your Progress

- 2 x 101 + 8 x 100 is equal to (a) 10 (b) 280 (c) 2.8 (d) 28
- The binary number 1101 is equal to the decimal number (a) 13 (b) 49 (c) 11 (d) 3
- The decimal 17 is equal to the binary number (a) 10010 (b) 11000 (c) 10001 (d) 01001
- The sum of 11010 + 01111 equals (a) 101001 (b) 101010 (c) 110101 (d) 101000
- The difference of 110 010 equals (a) 001 (b) 010 (c) 101 (d) 100
- The 1's complement of 10111001 is (a) 01000111 (b) 01000110 (c) 11000110 (d) 10101010
- The 2's complement of 11001000 is (a) 00110111 (b) 00110001 (c) 01001000 (d) 00111000
- The binary number 101100111001010100001 can be written in octal as
- (a) 54712308 (b) 54712418(c) 26345218 (d) 231625018
- The binary number 10001101010101011111 can be written in hexadecimal as
- (a)AD46716 (b) 8C46F16 (c) 8D46F16 (d) AE46F16
- The BCD number for decimal 473 is
- (a) 111011010 (b) 1110111110101001 (c) 010001110011 (d) 010011110011

Usage Notes

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Sincerely,

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